

# EEP 596: LLMs: From Transformers to GPT || Lecture 3

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Univ. of Washington, Seattle

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# Logistics

- Assignment 1 ✓
- Paper Presentation Slots Assignment ✓
- Assignment 2 ✓
- Anything else?

# Last Lecture

- History of Large Language Models
- LLM use-cases in the industry

# Today's Lecture

- Deep Learning Fundamentals

# Outline for Lecture

- Motivation for DL

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- DL Applications

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- Over-fitting and Hyper-parameters

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- Activation functions
- Tensorflow Demo
- Training and Back-propagation
- Over-fitting and Hyper-parameters
- Other DL architectures

# Deep Learning Reference

## Deep Learning

Great reference for the theory and fundamentals of deep learning: Book by Goodfellow and Bengio et al Bengio et al

Deep Learning History

# Introduction to Deep Learning

## Deep Learning

- 1 Lot of buzz around Deep Learning in the past decade and a half!

# Introduction to Deep Learning

## Deep Learning

- ① Lot of buzz around Deep Learning in the past decade and a half!
- ② Deep Learning refers to Neural Networks that is a loose approximation of how the brain works

# Applications of Deep Learning

## Applications

- 1 Self-driving cars

# Applications of Deep Learning

## Applications

- ① Self-driving cars 
- ② Sentiment analysis

# Applications of Deep Learning

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- ① Self-driving cars
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- ③ Text Summarization

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- ④ Arrhythmia detection - Possible assignment for this course!

# Applications of Deep Learning

## Applications

- 1 Self-driving cars
  - 2 Sentiment analysis
  - 3 Text Summarization
  - 4 Arrhythmia detection - Possible assignment for this course!
  - 5 Image to text generation. Caption images automatically.
- Handwritten notes in purple:*  
An arrow points from "Text Summarization" to "health work".  
Another arrow points from "health work" to "Arrhythmia detection".

# Applications of Deep Learning

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- ② Sentiment analysis
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# Applications of Deep Learning

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- ⑦ Auto-complete sentence in Emails. How many of us use this?

# Applications of Deep Learning

## Applications

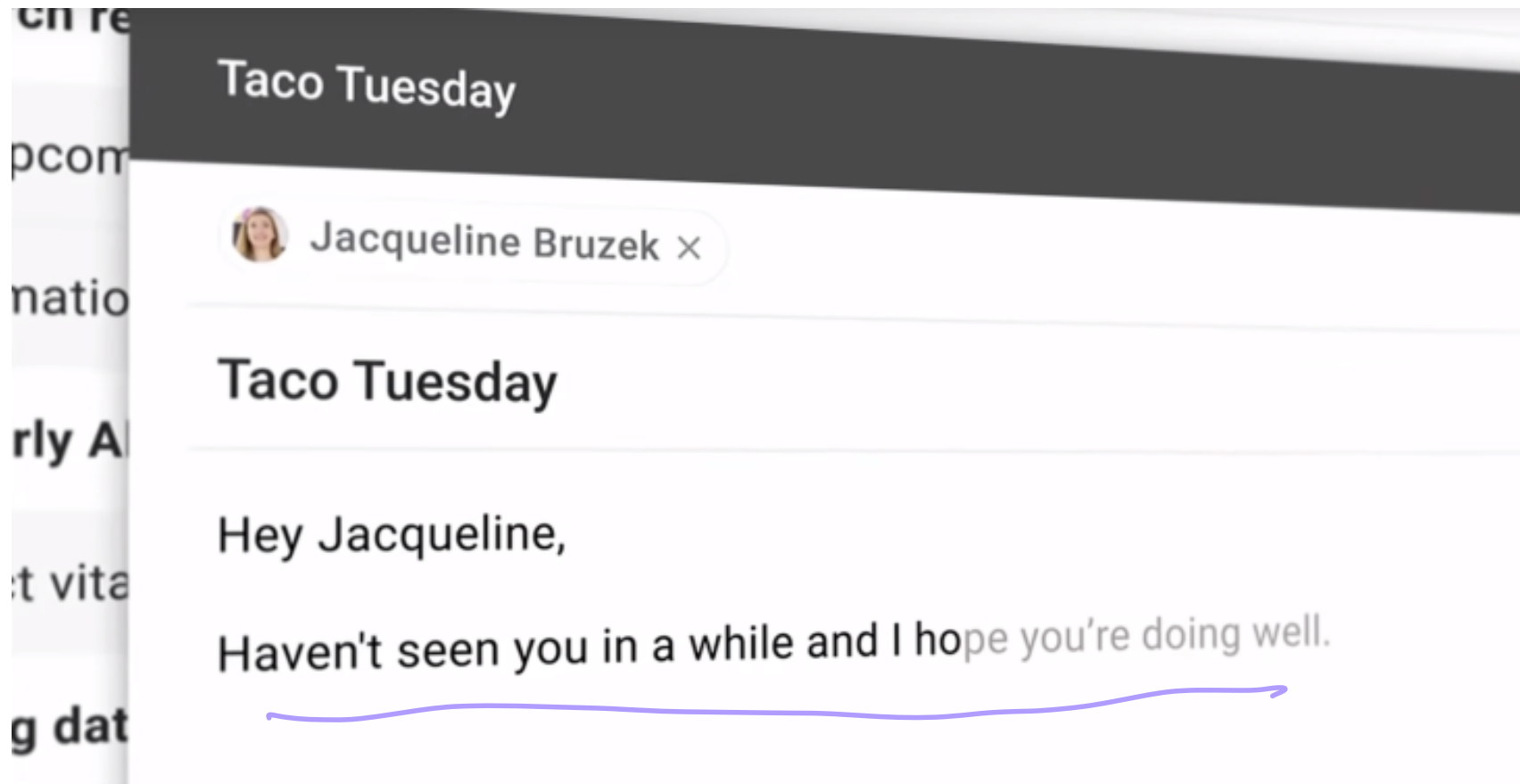
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- ⑧ Auto-complete search results.

# Applications of Deep Learning

## Applications

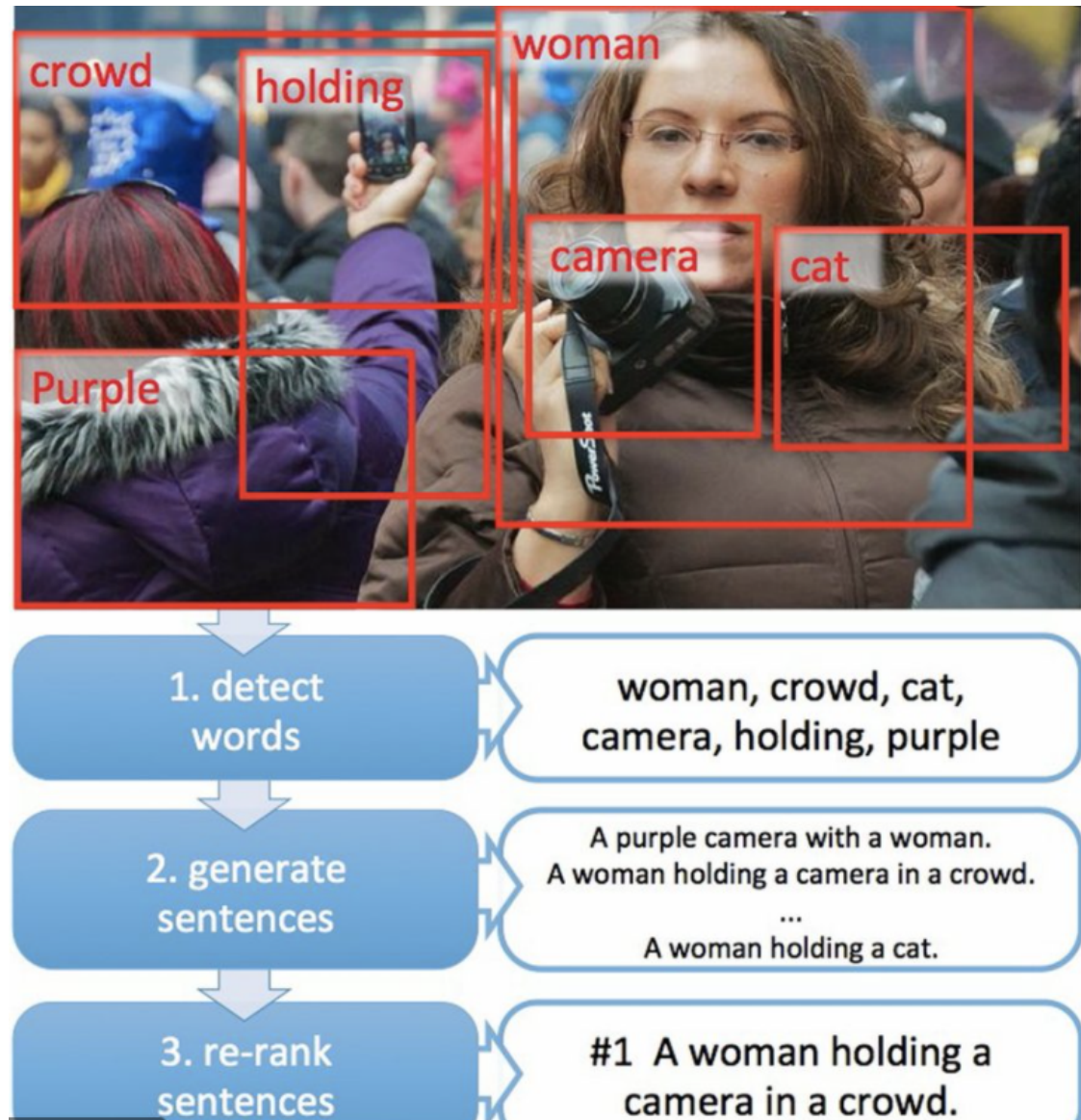
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- 7 Auto-complete sentence in Emails. How many of us use this?
- 8 Auto-complete search results.
- 9 Chat bots - Like ChatGPT/Sparrow/Anthropic, etc

# Email auto-complete

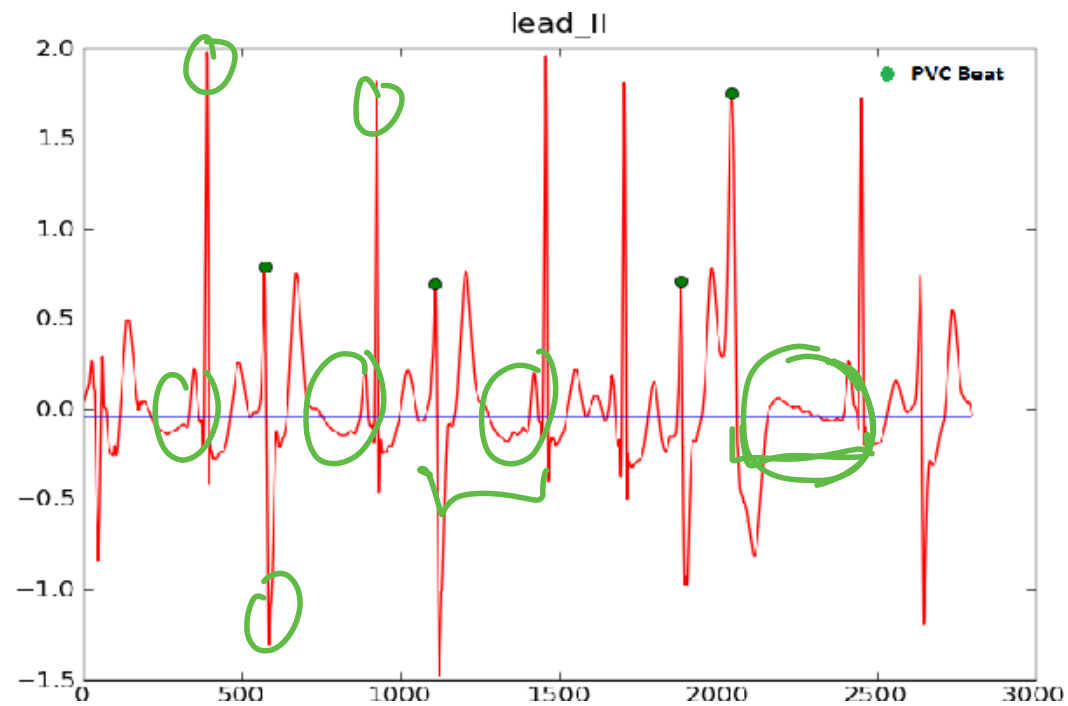


# Image to Text!

*inception*



# Arrhythmia Detection



Segment  
Anomalies

# Industry Applications (NLP focused)

- Tagging products at e-commerce companies with tags/category ids
- Coming up with category names, when none existed before
- Summarizing reviews for products
- Customer service help - Chatbots
- Live Speech Translation *Accent / Language Translation*
- Intent Recognition: Understanding intent behind a sentence or paragraph
- *Content Moderation* Detecting malicious intent and content in text (part of Responsible AI)
- Converting natural language instructions into SQL queries to run and respond back in natural language
- And many more!

# Brief History of Deep Learning

- **1965:** First deep-learning model came out in 1965 by Ivakhenko et al. Didn't use back-propagation for training but sequential least squares fit.
- **1979:** Earliest Convolutional Neural Network (CNN) by Fukushima et al.
- **1985:** Earliest back-propagation in 1985 by Hinton et al
- **1989:** Application of back-prop for recognizing MNIST hand-written digits at Bell labs by Yann LeCun
- **1993:** **LeNet** by Yann LeCun. The beginning of the **X-Nets** where X could be Alex, Inception, etc
- **1997:** Discovery of recurrent Neural Nets - RNN and LSTMs in 1997 by Hochreiter and Schmidhuber.

# Brief History of Deep Learning (and LLMs)

- 1997 - 2006: GPUs got faster - 1000x computational speed improvement
- 2011: Ciresan et al showed that you can train a CNN without pre-trained weights just with good computational power.
- 2012: Beginning of ILSVRC competition for improving image-net data set performance. *Manual Feature Eng. → Automated Feat. Eng.*
- 2017: Transformers arrive on the scene with Vaswani et al and begin the **Language Model revolution**.
- 2020: Transformer gets applied to Vision as well and matches CNN in performance through the Vi-Transformer.
- 2022: ChatGPT (based on transformers) arrives on the scene and puts AI on the world map!

# Brief History of Deep Learning (and LLMs)

- **2023:** Llama2 released with model weights (7b, 13b, 70b) by Meta and sees wider adoption as an open source alternative to ChatGPT. Context length of 4096 tokens
- **2024:** Llama3 released with 8b, 70b and 450b parameters. Context length of 8192 tokens but can extend to 128k tokens. Most popular and performant Meta model so far (unfortunately Llama4 didn't match expectations!)
- **2025:** DeepSeek releases their models with low-budget and architecture additions such as MLA and MOE, shaking up the industry and forcing big players to innovate!
- **2026:** Quest for super-intelligence continues as research explore multi-modal reasoning and mimicking how human brains work and reason with Thinking Machines and AML as examples
- **2026:** DeepSeek again releases a paper that doesn't just train existing transformers architecture on better data, but re-does the architecture for better results!

# Perceptron to Deep Neural Networks/Deep Learning

# Logistic Regression to Deep Learning

↓  
Linear

↓  
Non-linear

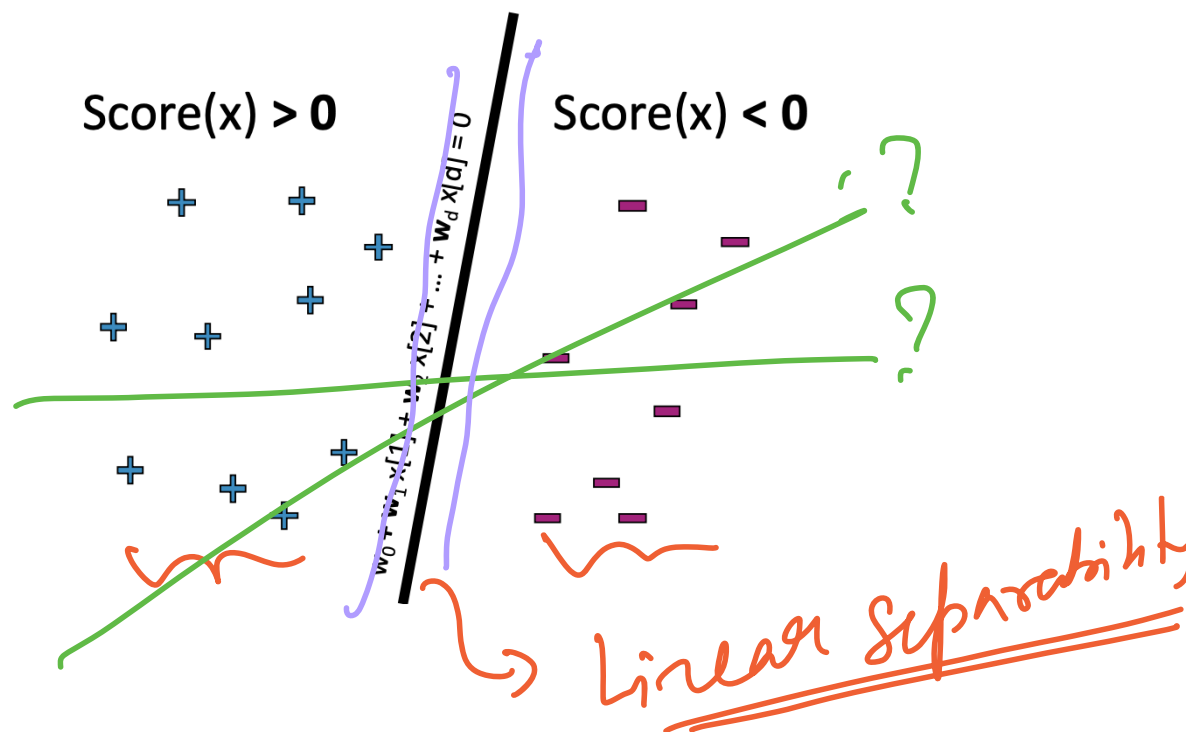
## Linear to Non-linear Models

Let's work through the nitty-gritties of the logistic regression model and neural network model!

# Perceptron

Single Neuron

$$\text{Score}(x) = w_0 + w_1 x[1] + w_2 x[2] + \dots + w_d x[d]$$



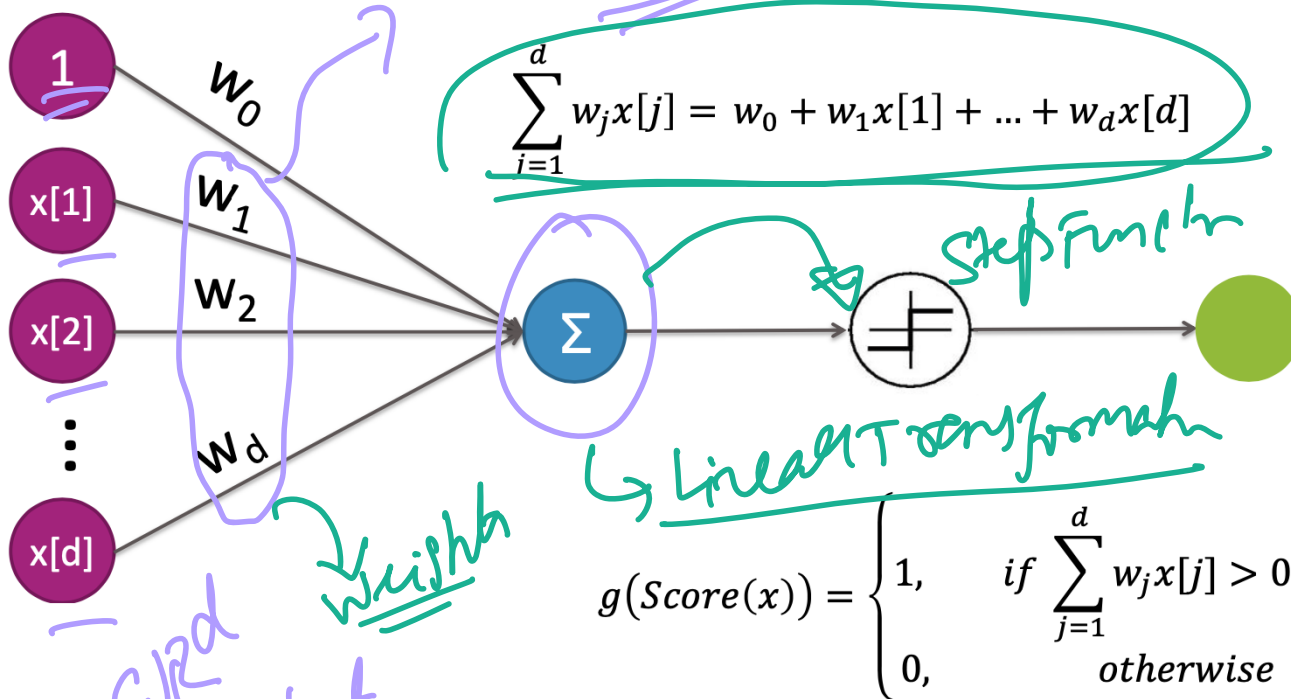
# Perceptron

Single Neuron

Ahead of time  
Trained by data

Input

Output



$x = \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_d \end{bmatrix} \in \mathbb{R}^d \rightarrow \text{Input}$

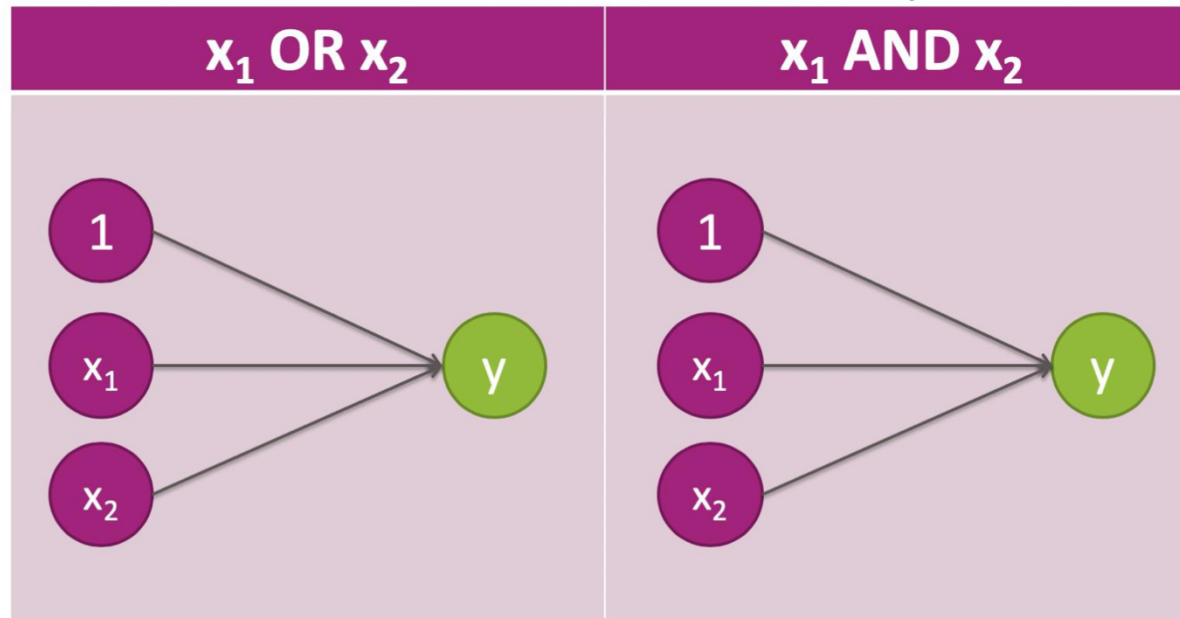
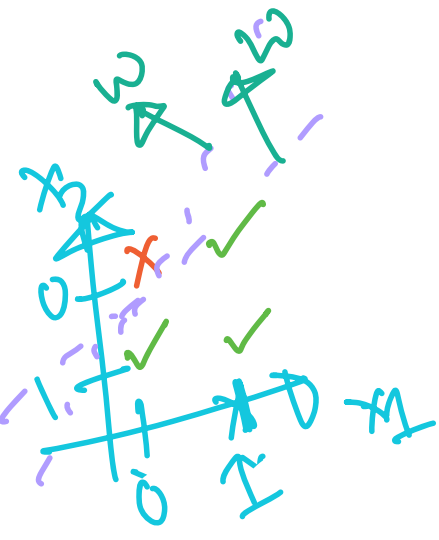
$\underline{\text{Input}}$

$\underline{\text{Weights}}$

$$g(\text{Score}(x)) = \begin{cases} 1, & \text{if } \sum_{j=1}^d w_j x[j] > 0 \\ 0, & \text{otherwise} \end{cases}$$

# OR and AND Functions

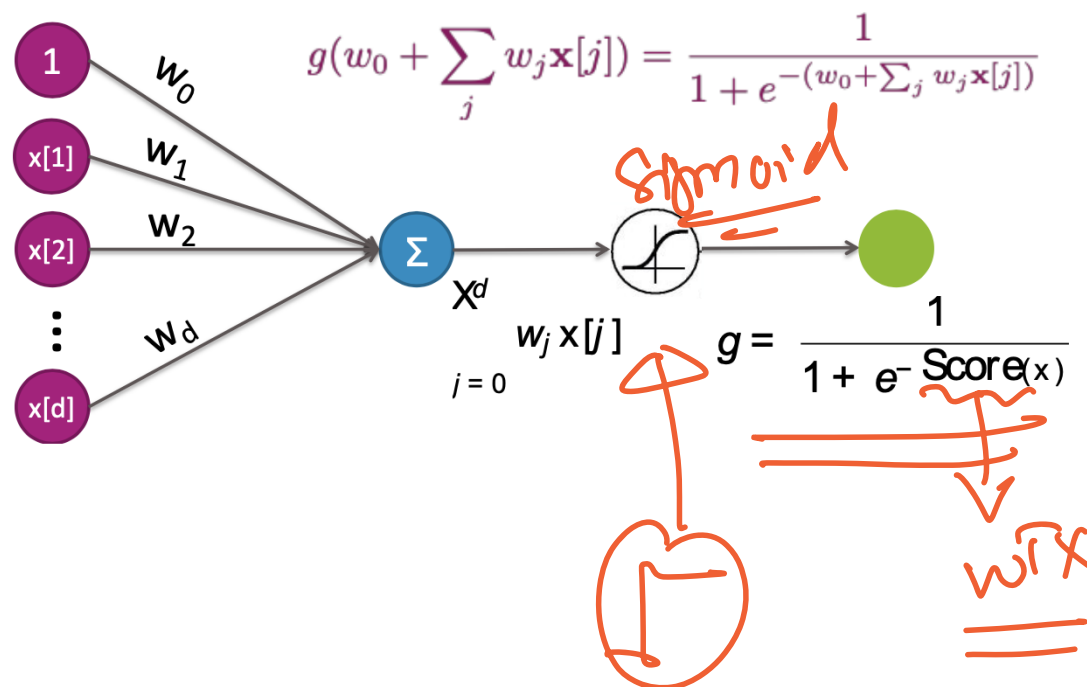
What can a perceptrons represent?



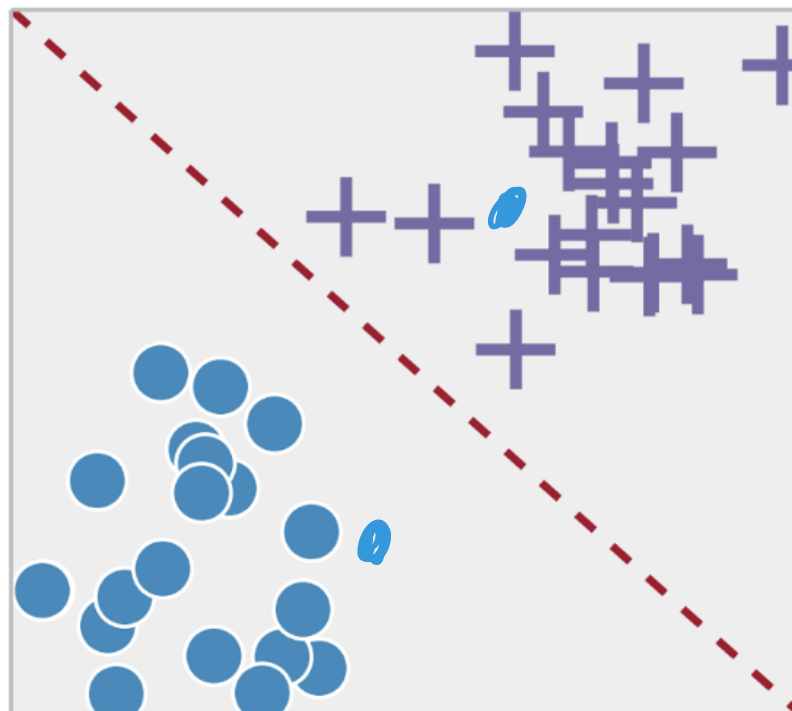
| $x_1$ | $x_2$ | $y$ |
|-------|-------|-----|
| 0     | 0     | 0   |
| 0     | 1     | 1   |
| 1     | 0     | 1   |
| 1     | 1     | 1   |

| $x_1$ | $x_2$ | $y$ |
|-------|-------|-----|
| 0     | 0     | 0   |
| 0     | 1     | 0   |
| 1     | 0     | 0   |
| 1     | 1     | 1   |

# Perceptron to Logistic Regression



# Logistic Regression



## LR fundamentals

- Linear Model
- Want score  $w^T x^i > 0$  for  $y_i = +1$  and  $w^T x_i < 0$  for  $y_i = -1$ !
- If linearly separable data, above is feasible. Else, minimize error in separability!!

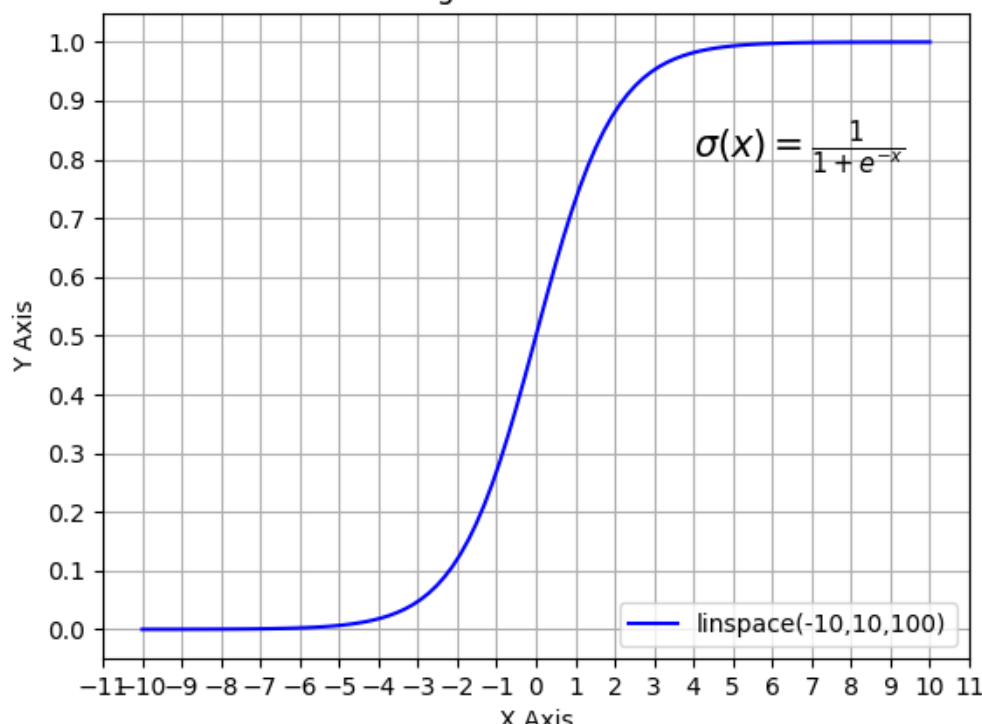
# Logistic Regression

## Probability for a class

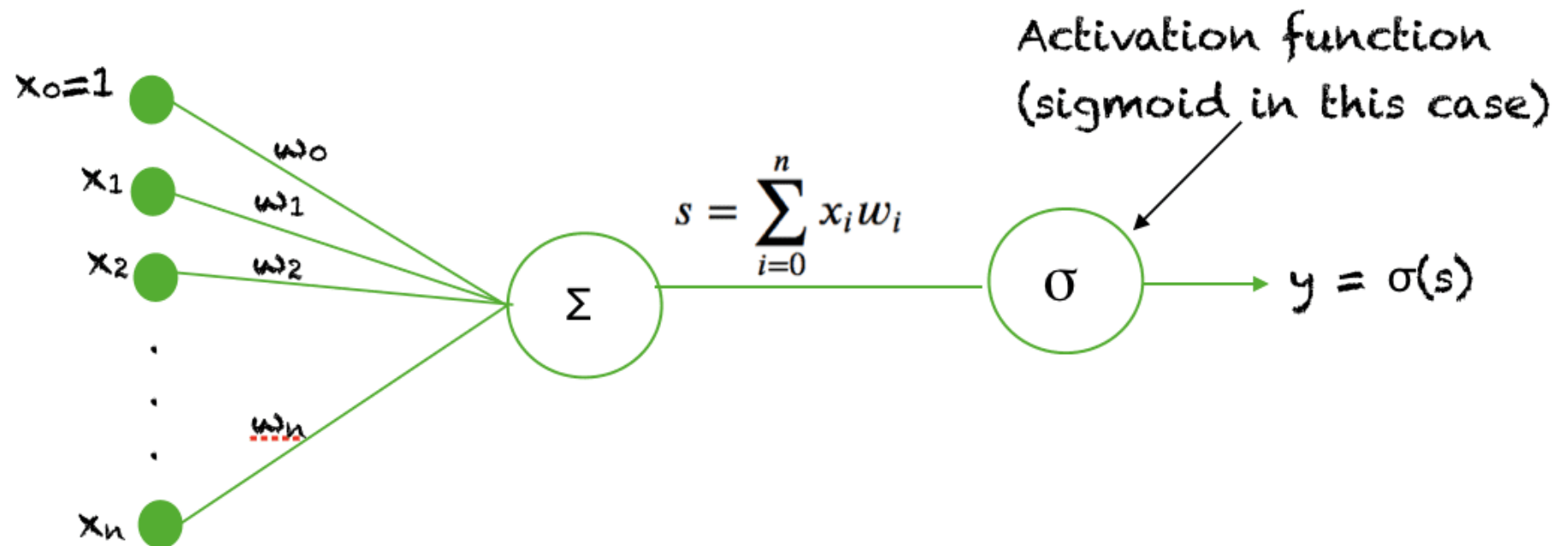
In LR, the score,  $w^T x$  is converted to a probability through the sigmoid function. So we can talk about  $P(\hat{y}^i = +1)$  or  $P(\hat{y}^i = -1)$

## Sigmoid Function

Sigmoid  
Sigmoid Function



# LR represented Graphically



# ICE #1

Compute  $w^T x$  for  $w = [1, 2, 3]$  and  $x = [-1, 1, 2]$

- 1 5
- 2 6
- 3 7
- 4 8

# Logistic Regression

## LR Prediction

$$\hat{y}_i = \left( \frac{1}{1 + e^{-\hat{w}^T x^i}} \right)$$

$\hat{y}_i = 0$   
and  $\hat{y}_i = 1$

loss = +∞

Score

## LR Loss

Assume that  $y_i = 0$  or  $y_i = 1$  (i.e. the negative class has a label 0).

Then the binary cross-entropy loss applies to LR:

$$\min_w -y_i \log(\hat{y}_i) - (1 - y_i) \log(1 - \hat{y}_i)$$

$(y_i \log(\hat{y}_i) = 1 \cdot \log(1))$

$y_i \log(\hat{y}_i) = 1 \log(1) = 0$

## ICE #2

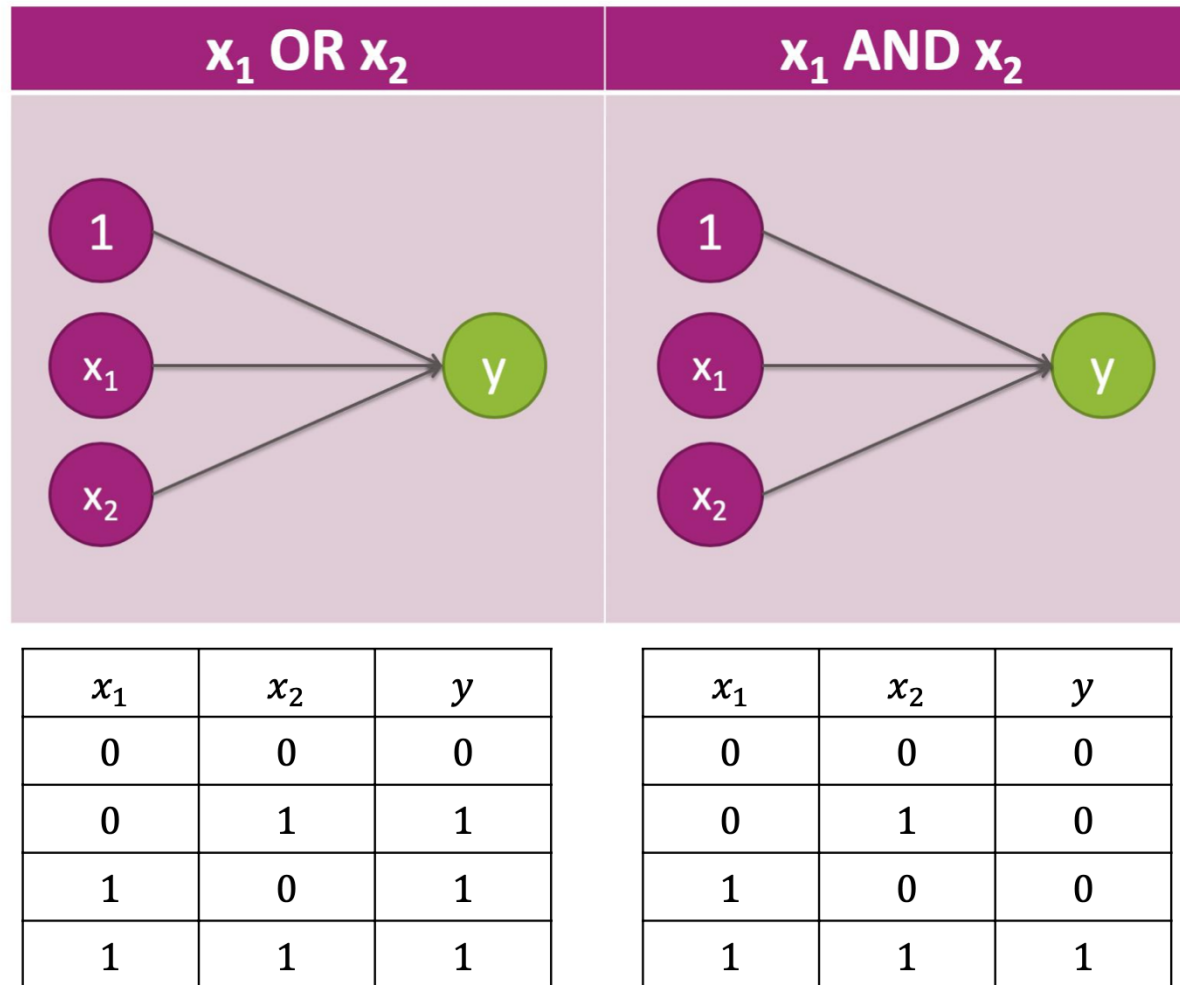
If log is to the base 2, what is the value of binary-cross entropy at a ground truth of 1 and prediction label of 0.5? Binary cross-entropy is given by,

$$-y_i \log(\hat{y}_i) - (1 - y_i) \log(1 - \hat{y}_i)$$

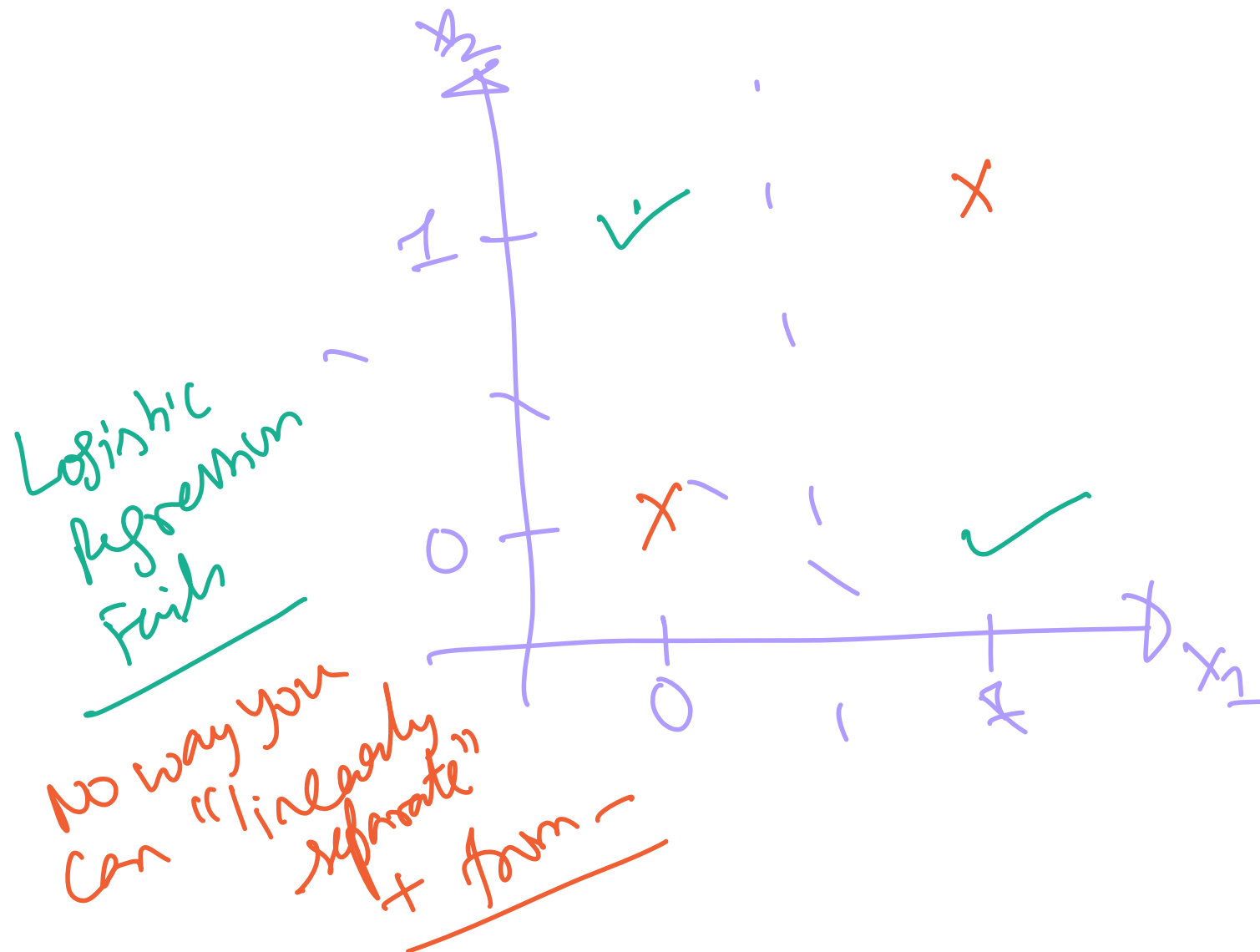
- ① 0
- ② 0.5
- ③ 1
- ④ 2

# OR and AND Functions

What can a perceptrons represent?



# Learning XOR



# XOR through Multi-layer perceptron

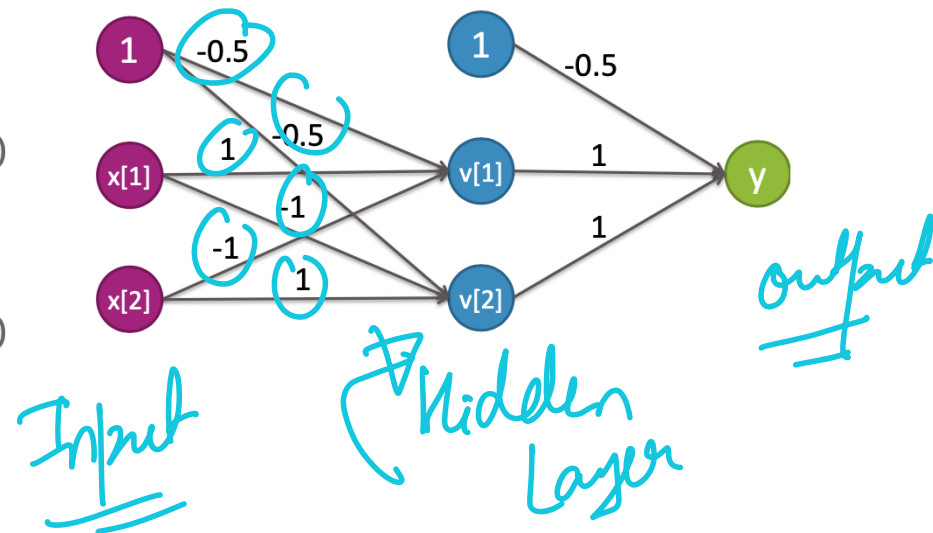
This is a 2-layer neural network

$$y = x[1] \text{ XOR } x[2] = (x[1] \text{ AND } \neg x[2]) \text{ OR } (\neg x[1] \text{ AND } x[2])$$

$$\begin{aligned} v[1] &= (x[1] \text{ AND } \neg x[2]) \\ &= g(-0.5 + x[1] - x[2]) \end{aligned}$$

$$\begin{aligned} v[2] &= (\neg x[1] \text{ AND } x[2]) \\ &= g(-0.5 - x[1] + x[2]) \end{aligned}$$

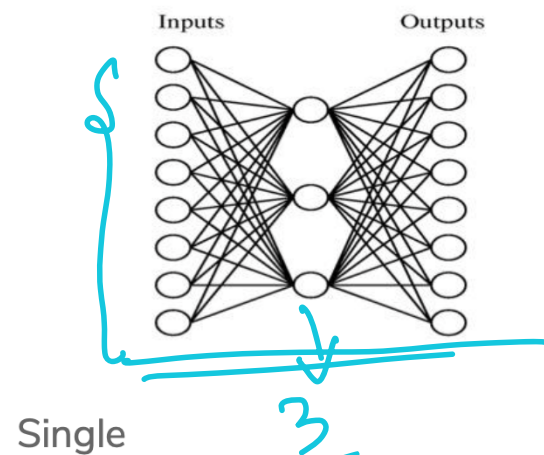
$$\begin{aligned} y &= v[1] \text{ OR } v[2] \\ &= g(-0.5 + v[1] + v[2]) \end{aligned}$$



$x_1$      $x_2$      $v_1$      $v_2$      $y$   
 0 1 0 1 0  
 1 0 1 0 1

# 2 Layer Neural Network

Two layer neural network (alt. one hidden-layer neural network)



$$out(x) = g\left(w_0 + \sum_j w_j x[j]\right)$$

1-hidden layer

$$out(x) = g\left(w_0 + \sum_k w_k g\left(w_0^{(k)} + \sum_j w_j^{(k)} x[j]\right)\right)$$

Handwritten notes in purple ink:

- step
- Sigmoid
- ReLU
- Activation Function

# ICE #3

Which methods can learn the XOR function?

- ① Logistics Regression ✗
- ② Naive Bayes Classifier ? ✗
- ③ Decision Trees ✓
- ④ Support Vector Machines ✗

# Deep Learning: Activations, FFN and more

# Choices for Non-Linear Activation Function

- **Sigmoid**

- Historically popular, but (mostly) fallen out of favor
- Neuron's activation saturates (weights get very large  $\rightarrow$  gradients get small)
- Not zero-centered  $\rightarrow$  other issues in the gradient steps
- When put on the output layer, called "softmax" because interpreted as class probability (soft assignment)

- **Hyperbolic tangent**  $g(x) = \tanh(x)$

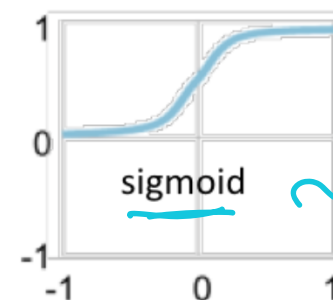
- Saturates like sigmoid unit, but zero-centered

- **Rectified linear unit (ReLU)**  $g(x) = x^+ = \max(0, x)$

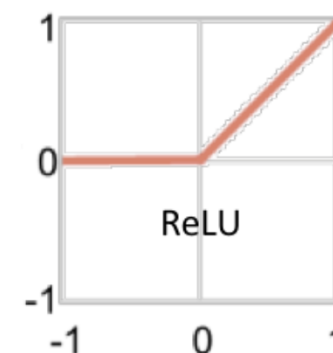
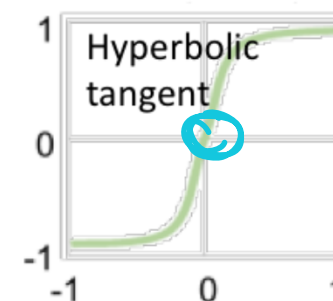
- Most popular choice these days
- Fragile during training and neurons can "die off"... be careful about learning rates
- "Noisy" or "leaky" variants

- **Softplus**  $g(x) = \log(1 + \exp(x))$

- Smooth approximation to rectifier activation

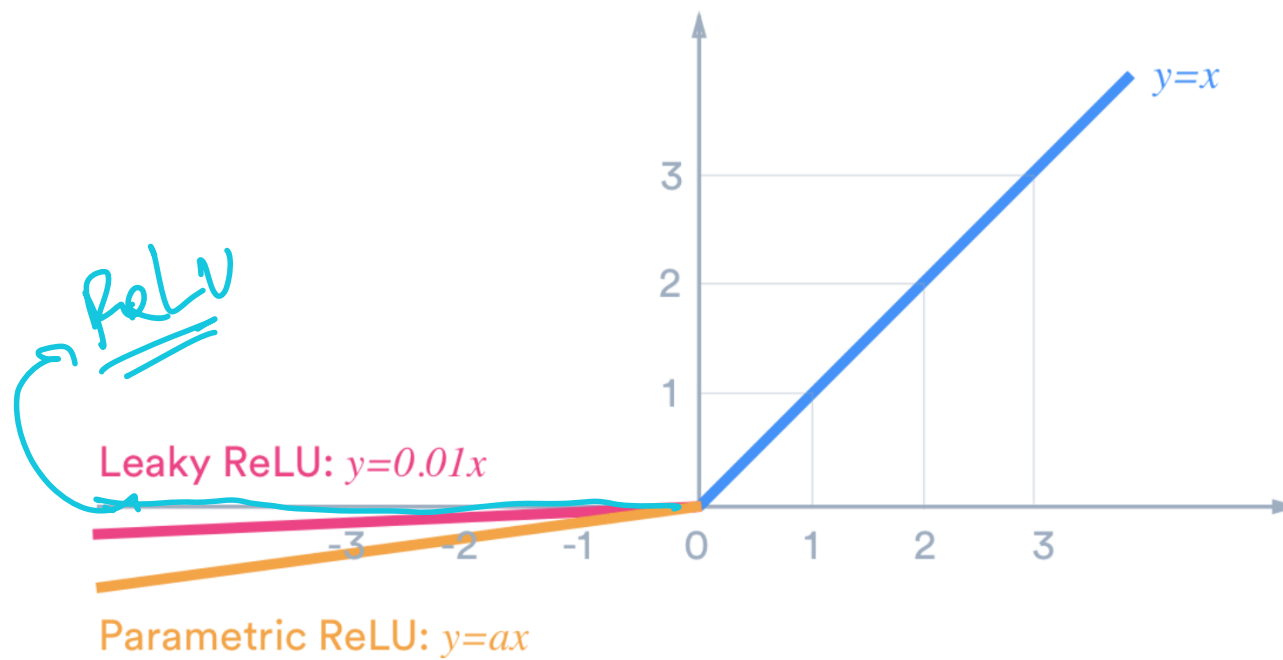


softmax

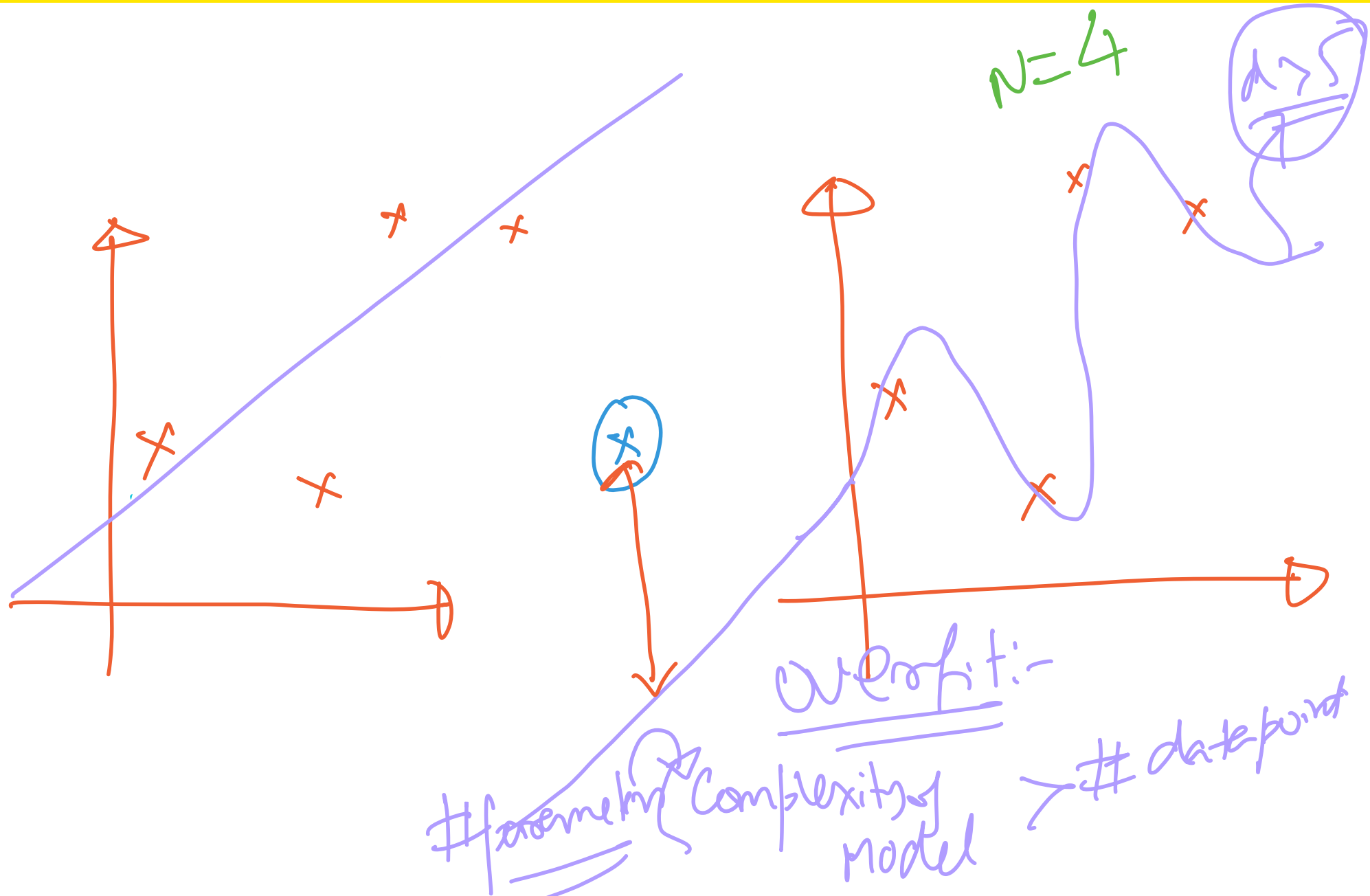


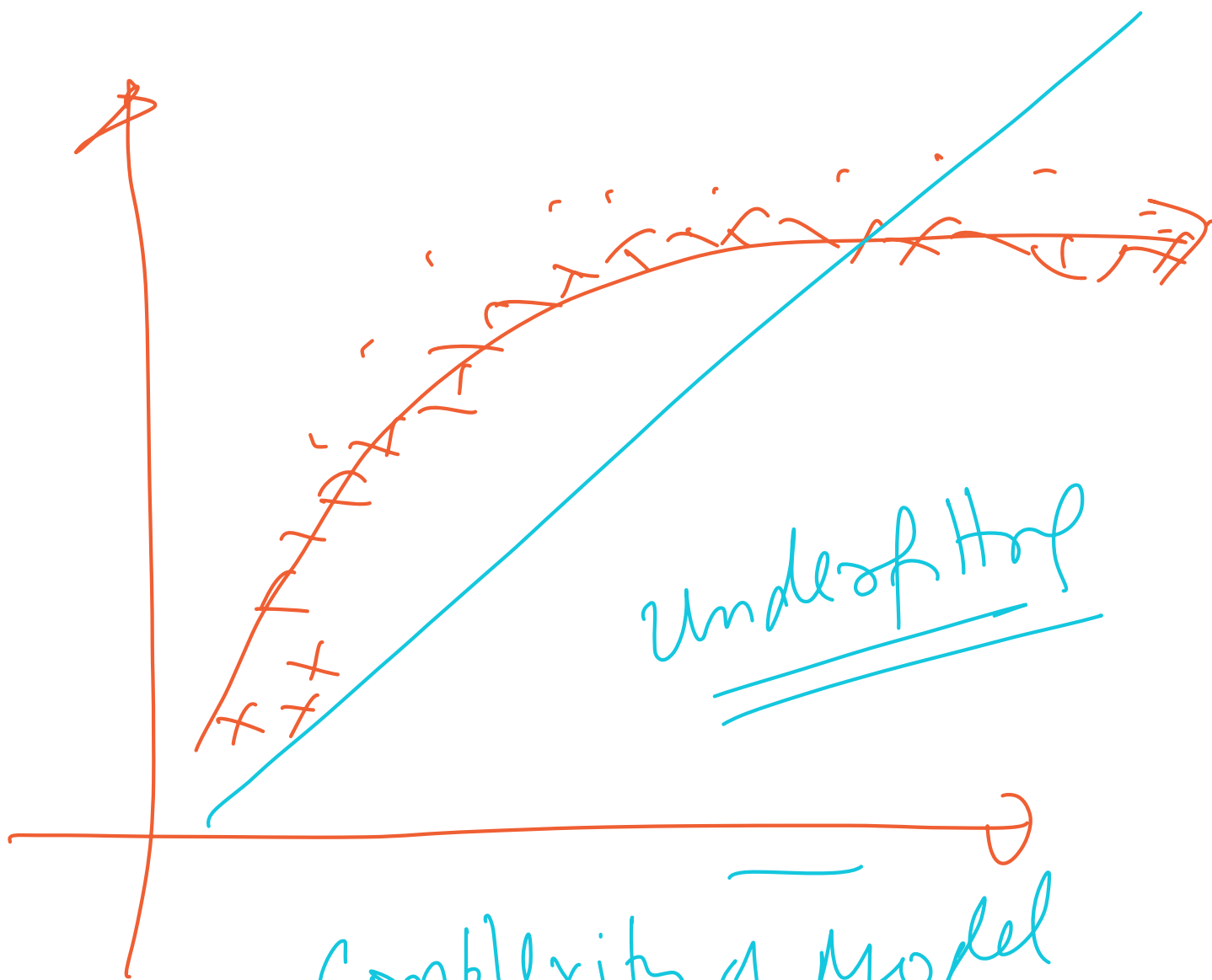
# Sigmoid vs RELU

# RELU vs Leaky RELU



# Phenomenon of Overfitting





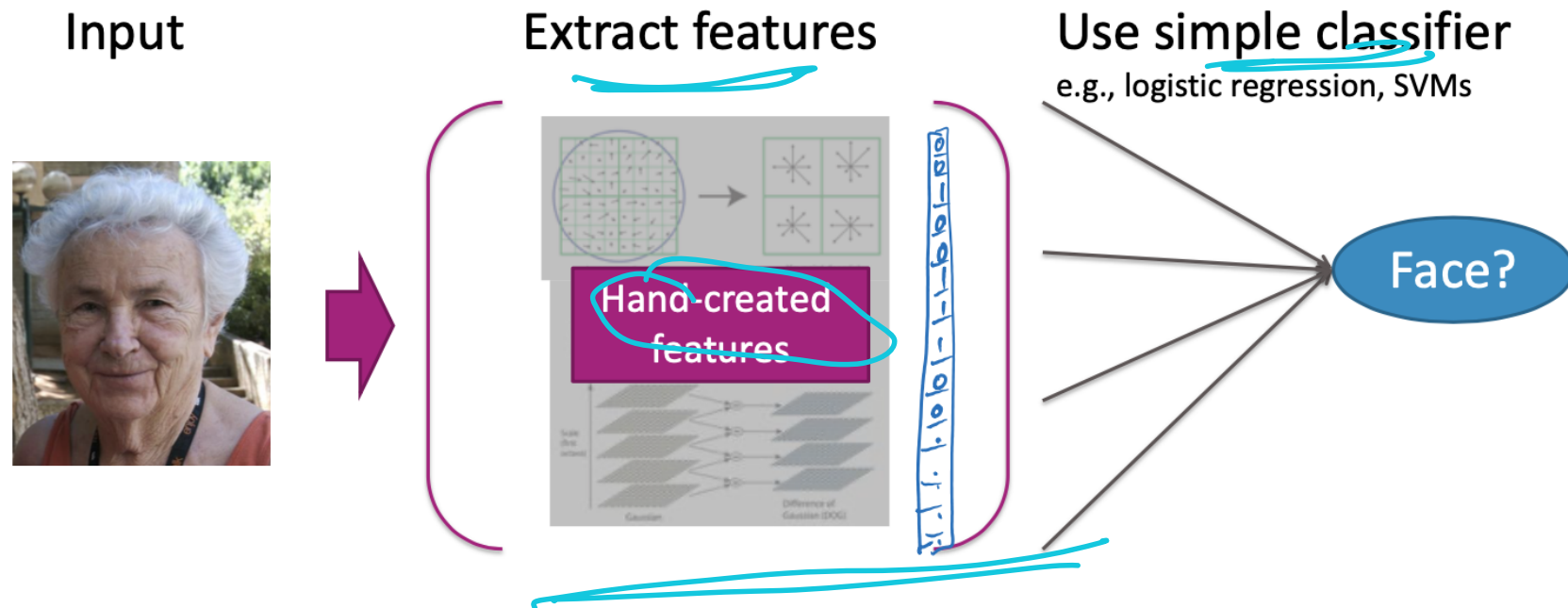
Complexity of Model  
Can be higher

# Tensorflow Playground Demo

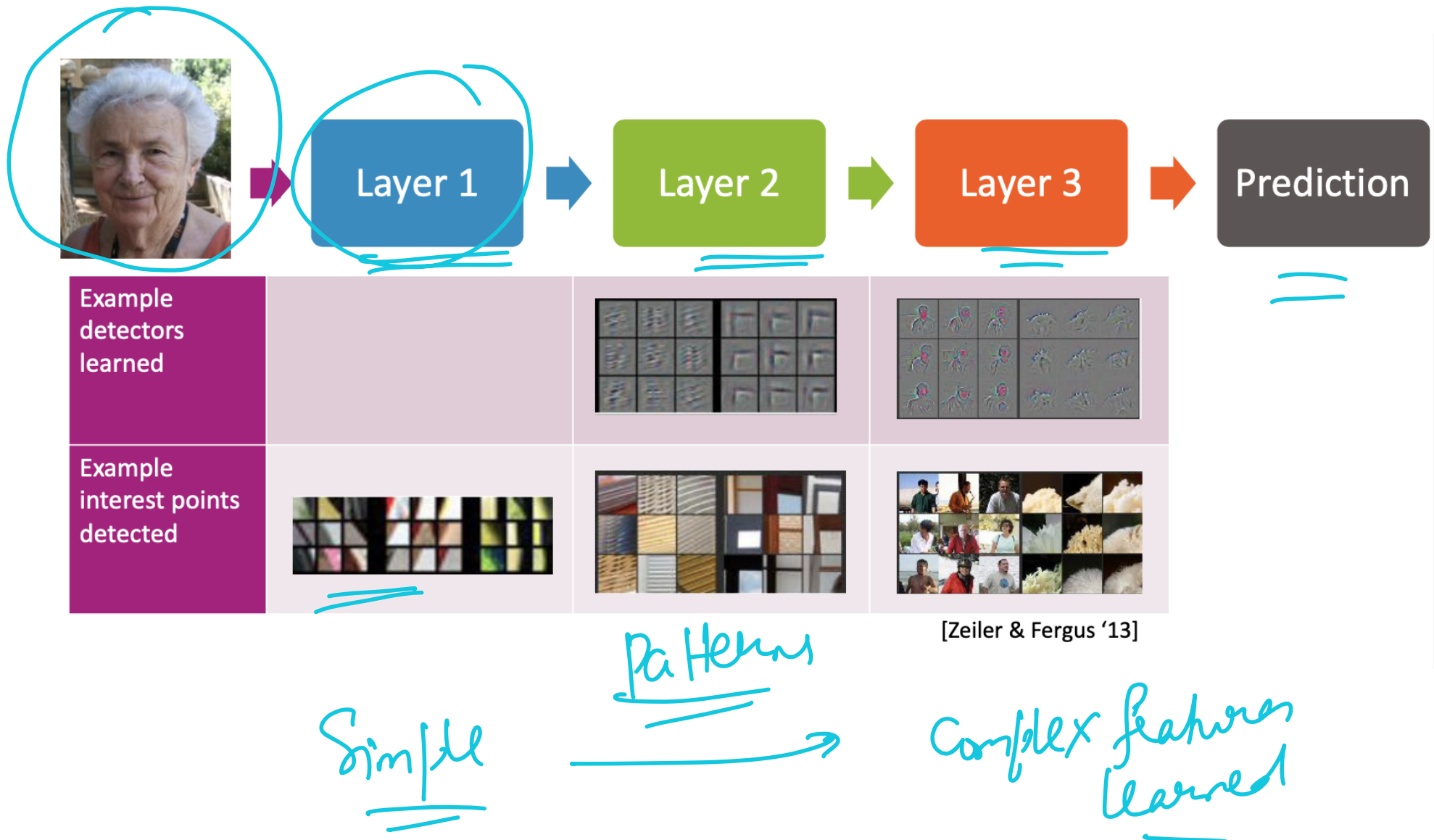


Tensorflow Playground Demo

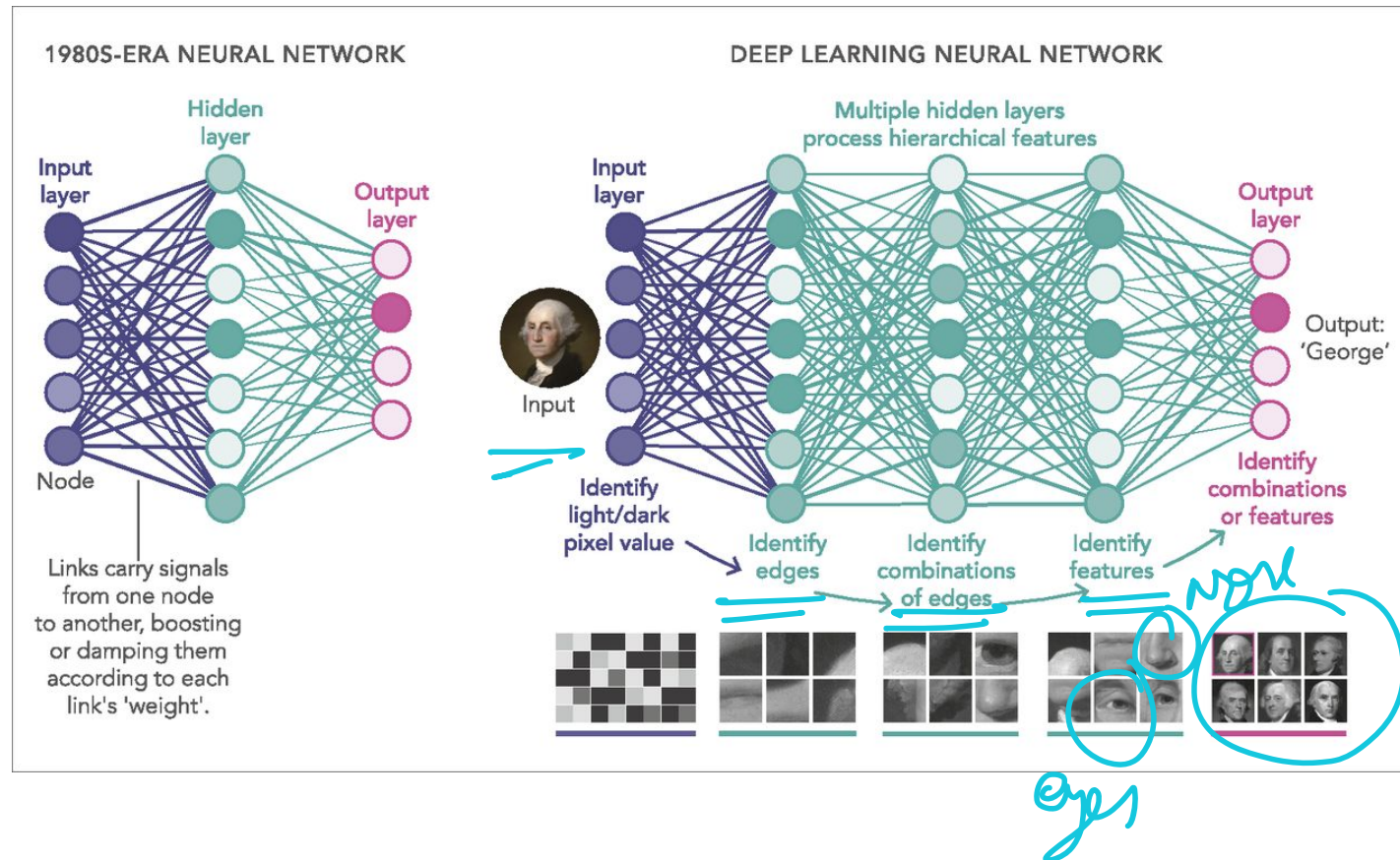
# Computer vision before deep learning



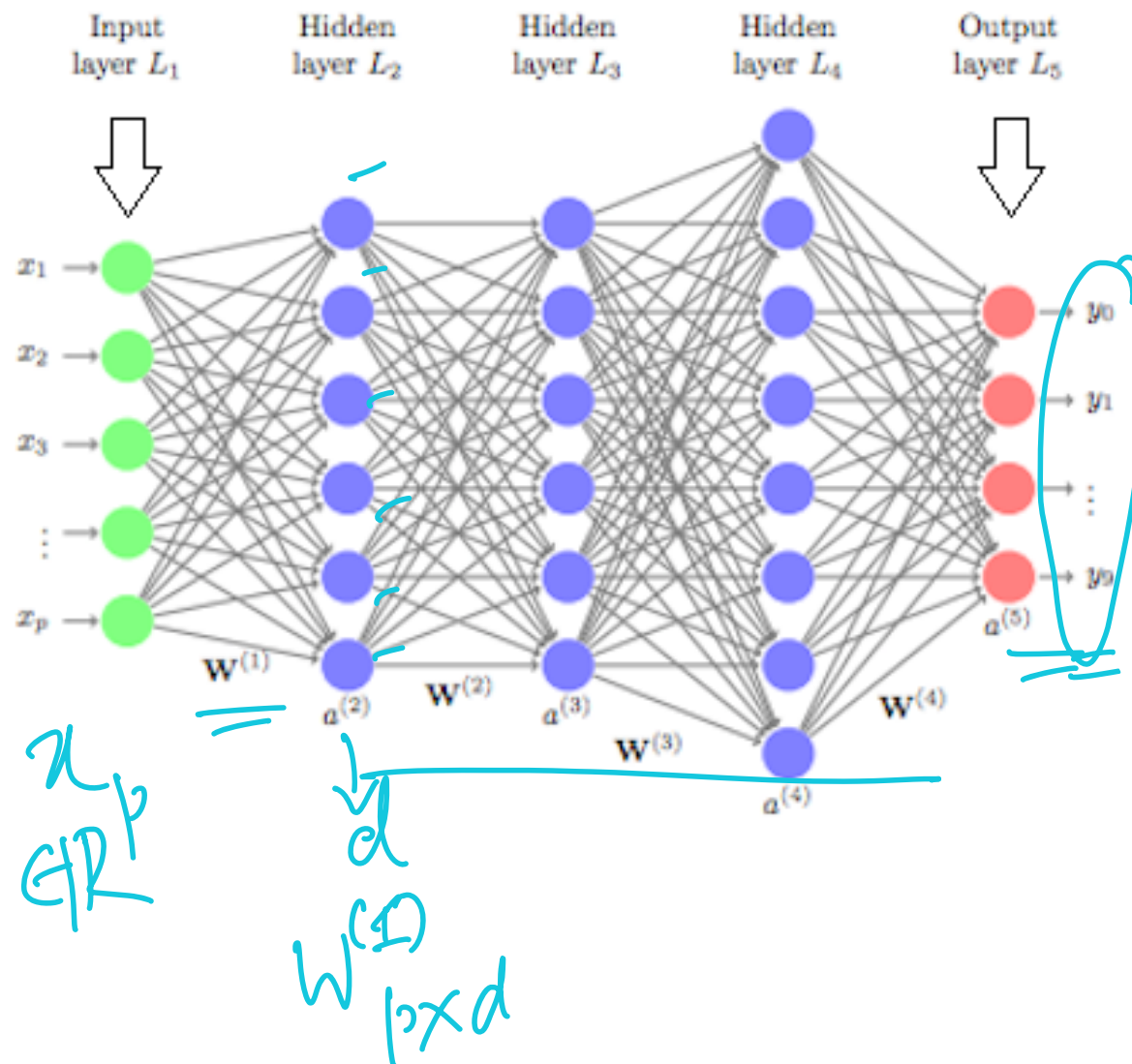
# Computer vision after deep learning



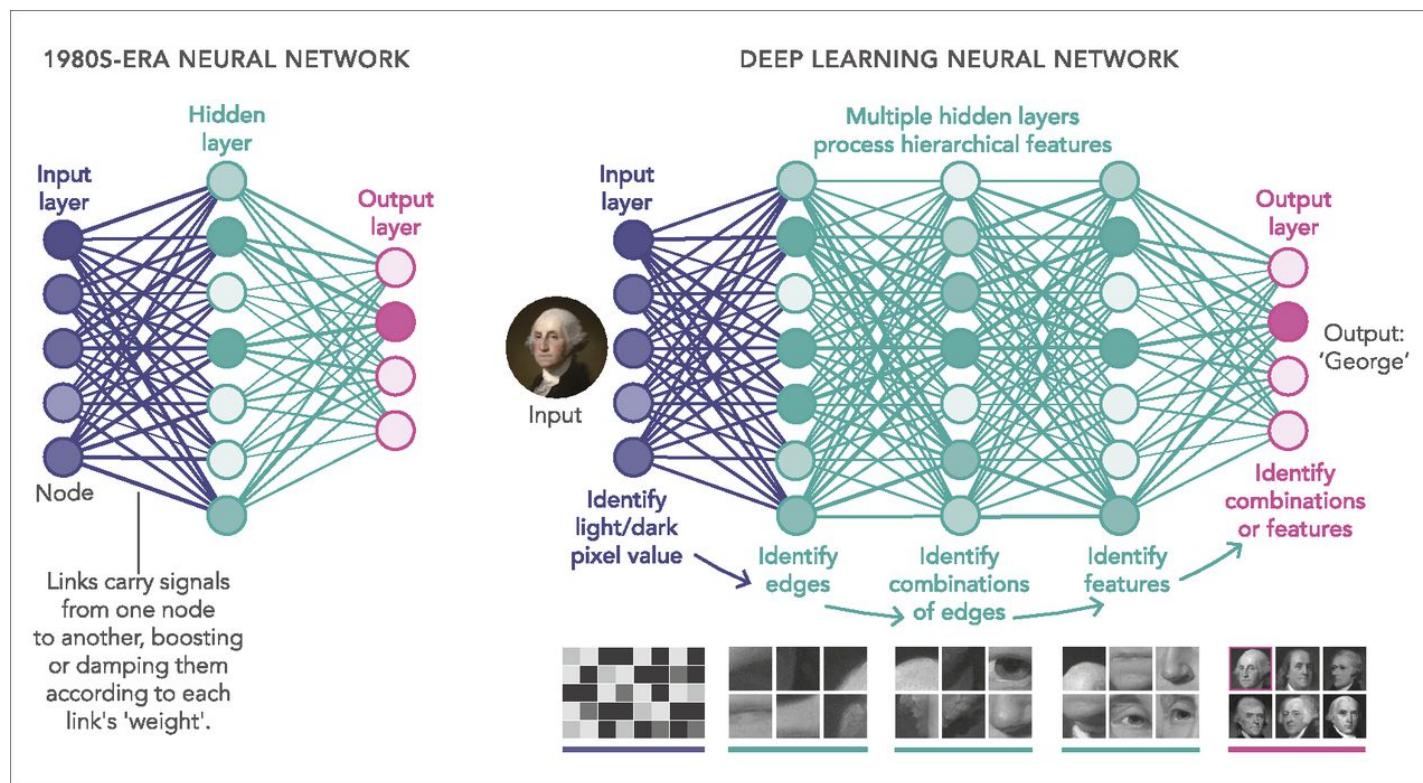
# Feed-forward Deep Learning Architecture Example



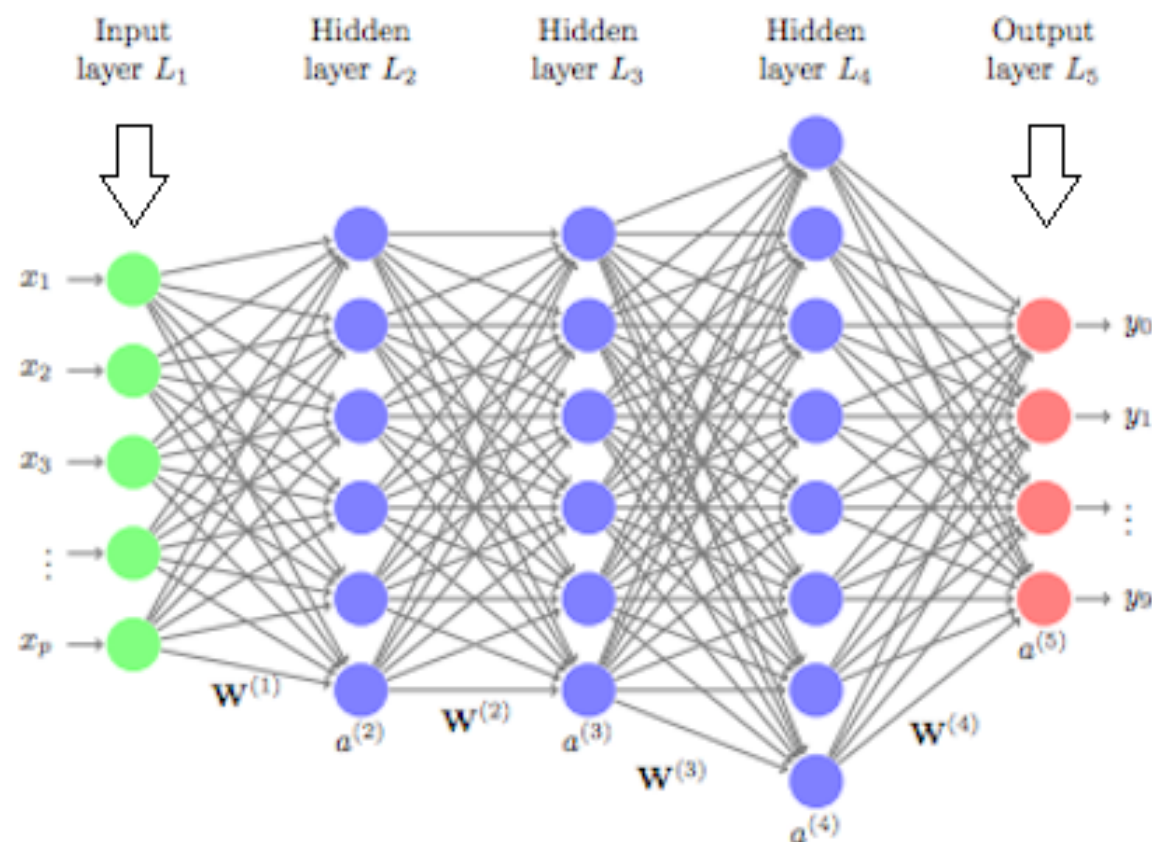
# Feed-forward Deep Learning Architecture Example



# Feed-forward Deep Learning Architecture Example



# Feed-forward Deep Learning Architecture Example



# ICE #4



Compute the number of parameters in DNN model

Consider a DNN model with 3 hidden layers where each hidden layer has 1000 neurons. Let the input layer be raw pixels from a 100x100 image and the output layer has 10 dimensions, let's say for a 10 class image classification example. How many total parameters exist in the DNN model?

- ① 10 million parameters
- ② 11 million parameters
- ③ 12 million parameters
- ④ 13 million parameters

# Training a DNN

## SGD with mini-batch

SGD mini-batch is the staple diet. However there are some **learning rate schedulers** that are known to work better for DNNs - Such as Adagrad and more recently, ADAM. ADAM adapts the learning rate to each individual parameter instead of having a global learning rate.

# Training a DNN

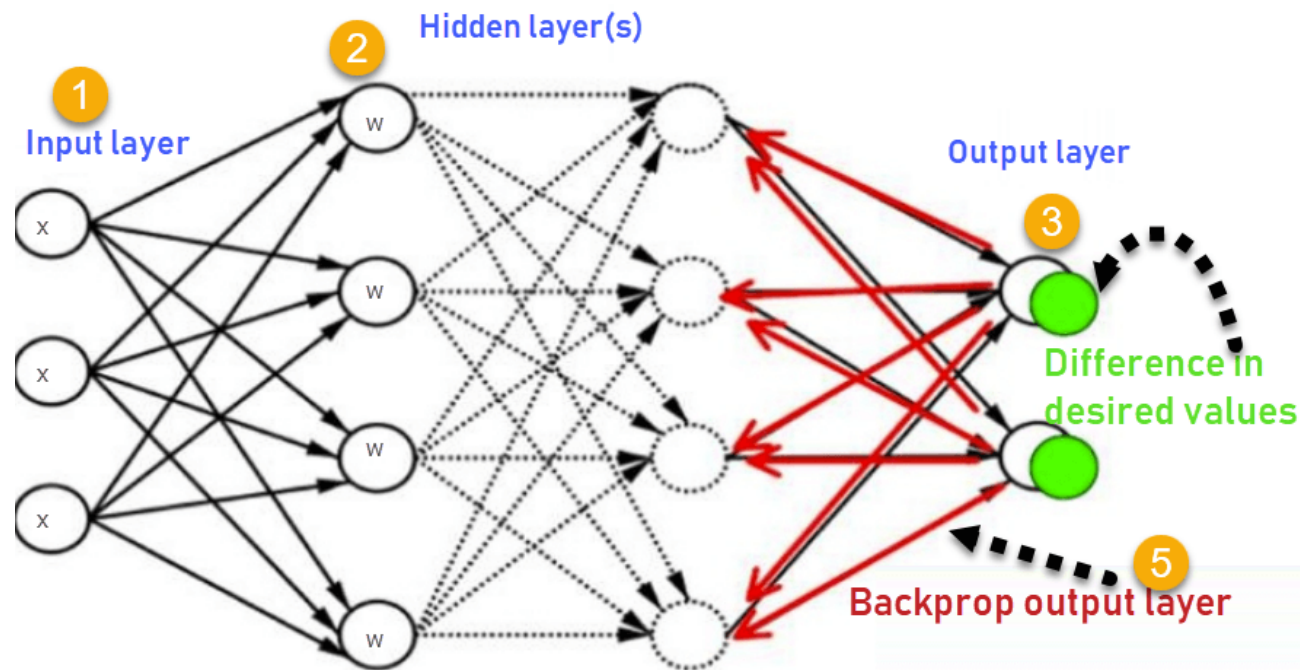
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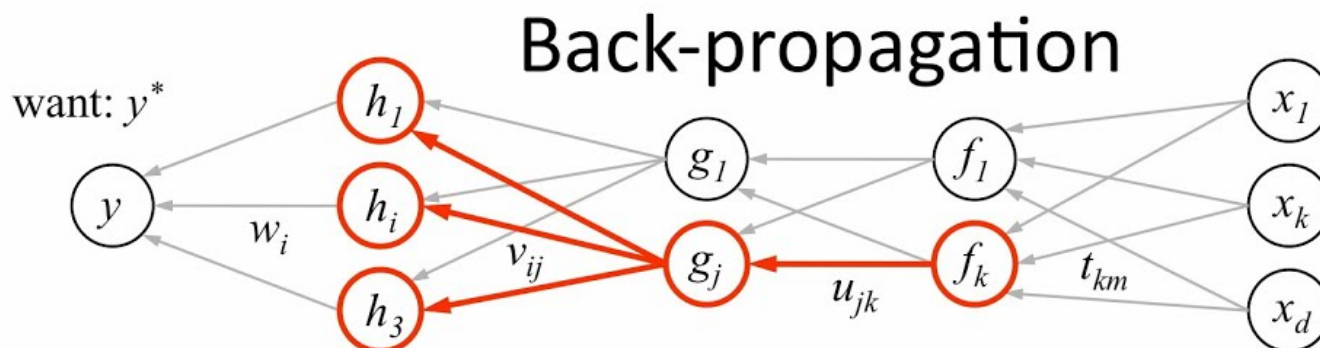
How do we compute gradient in a DNN?

Back-propagation!

# Forward Propagation vs Back-propagation



# Back Propagation explained



1. receive new observation  $\mathbf{x} = [x_1 \dots x_d]$  and target  $y^*$
2. **feed forward:** for each unit  $g_j$  in each layer  $1 \dots L$   
compute  $g_j$  based on units  $f_k$  from previous layer:  $g_j = \sigma \left( u_{j0} + \sum_k u_{jk} f_k \right)$
3. get prediction  $y$  and error  $(y - y^*)$
4. **back-propagate error:** for each unit  $g_j$  in each layer  $L \dots 1$

(a) compute error on  $g_j$

$$\underbrace{\frac{\partial E}{\partial g_j}}_{\text{should } g_j \text{ be higher or lower?}} = \sum_i \underbrace{\sigma'(h_i)}_{\text{how } h_i \text{ will change as } g_j \text{ changes}} \underbrace{v_{ij}}_{\text{was } h_i \text{ too high or too low?}} \underbrace{\frac{\partial E}{\partial h_i}}_{\text{was } h_i \text{ too high or too low?}}$$

(b) for each  $u_{jk}$  that affects  $g_j$

(i) compute error on  $u_{jk}$

$$\frac{\partial E}{\partial u_{jk}} = \underbrace{\frac{\partial E}{\partial g_j}}_{\text{do we want } g_j \text{ to be higher/lower}} \underbrace{\sigma'(g_j) f_k}_{\text{how } g_j \text{ will change if } u_{jk} \text{ is higher/lower}}$$

(ii) update the weight

$$u_{jk} \leftarrow u_{jk} - \eta \frac{\partial E}{\partial u_{jk}}$$

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# Back Propagation Summary

## Back Prop

Back prop is one of the fundamental backbones of the training modules behind deep learning and beyond (including for example ChatGPT). What exactly is back prop? It is just a way to unravel gradient computation in the neural network. Back prop is how we would **compute the gradient** in a neural network.

# Back Propagation Summary

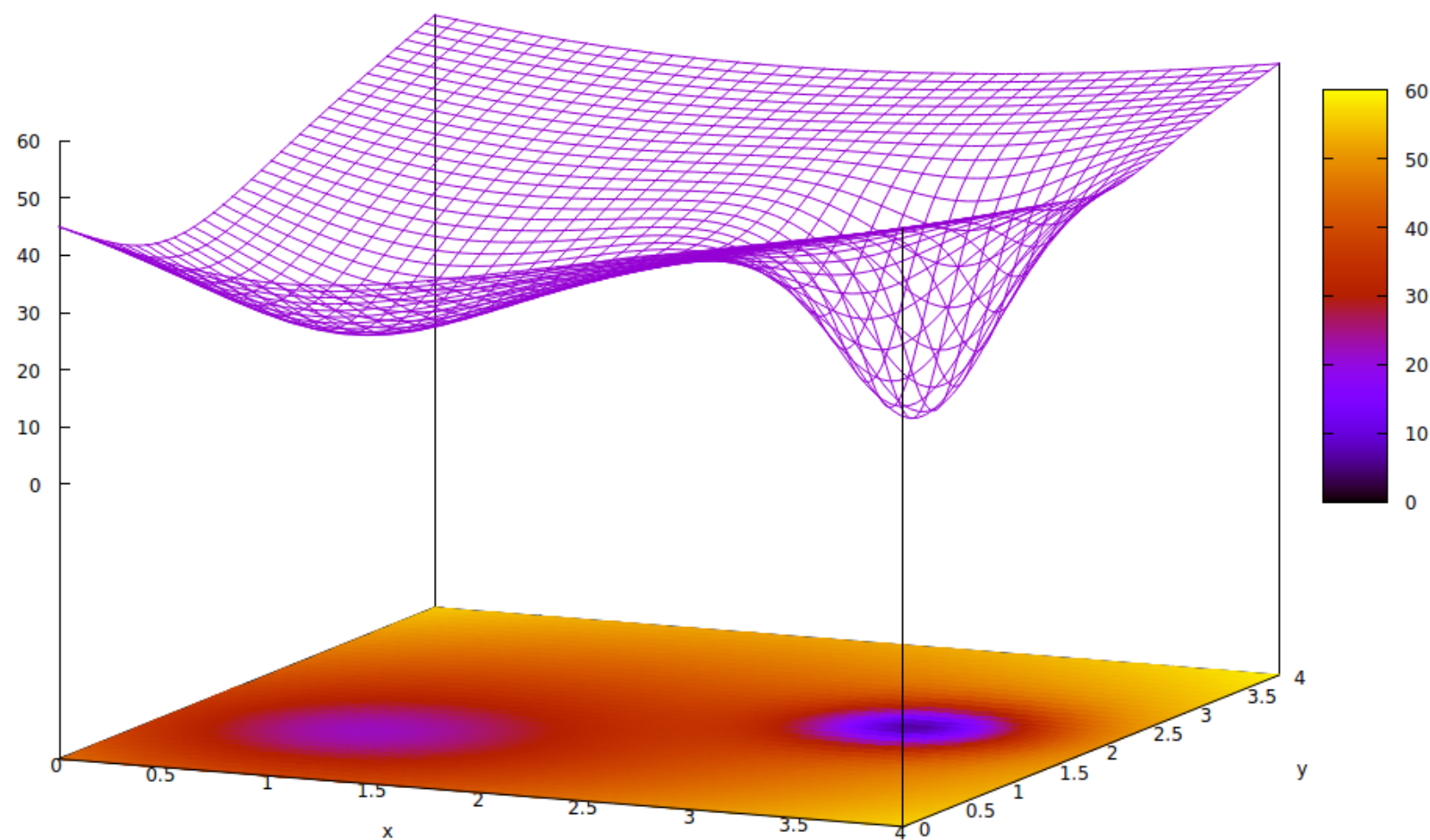
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## Back Prop as information flow

It can also be thought of as flow information from the error in the output (the loss function) down to the weights. Update the weights so we don't make **this error** next time around. Back prop is a way to do **gradient descent in neural networks!**

# Good vs Bad Local minima



# Hyper-parameters in Deep Learning

ICE #5: Which of the following is not a hyper-parameter in deep learning?

- ① Learning rate
- ② Number of Hidden Layers
- ③ Number of neurons per hidden layer
- ④ All of the above

# Hyper-parameters in Deep Learning

## Hyper-parameters

- ① Learning rate
- ② Number of Hidden Layers
- ③ Number of neurons per hidden layer

# Hyper-parameters in Deep Learning

## Hyper-parameters

- ① Learning rate
- ② Number of Hidden Layers
- ③ Number of neurons per hidden layer
- ④ Type of non-linear activation function used

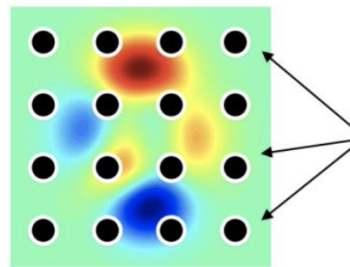
# Hyper-parameters in Deep Learning

## Hyper-parameters

- ① Learning rate
- ② Number of Hidden Layers
- ③ Number of neurons per hidden layer
- ④ Type of non-linear activation function used
- ⑤ Anything else?

# Hyper-parameter tuning methods

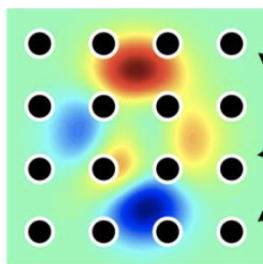
Grid search:



Hyperparameters  
on 2d uniform grid

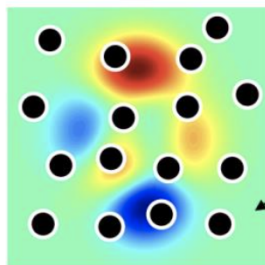
# Hyper-parameter tuning methods

Grid search:



Hyperparameters  
on 2d uniform grid

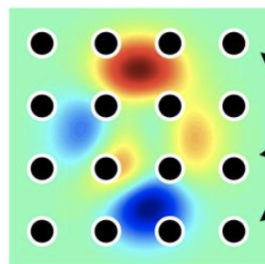
Random search:



Hyperparameters  
randomly chosen

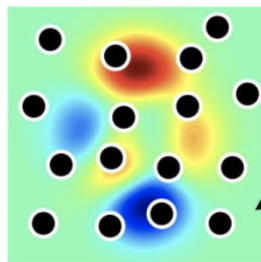
# Hyper-parameter tuning methods

Grid search:



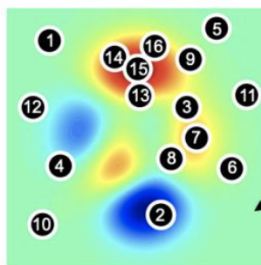
Hyperparameters  
on 2d uniform grid

Random search:



Hyperparameters  
randomly chosen

Bayesian Optimization:



Hyperparameters  
**adaptively** chosen

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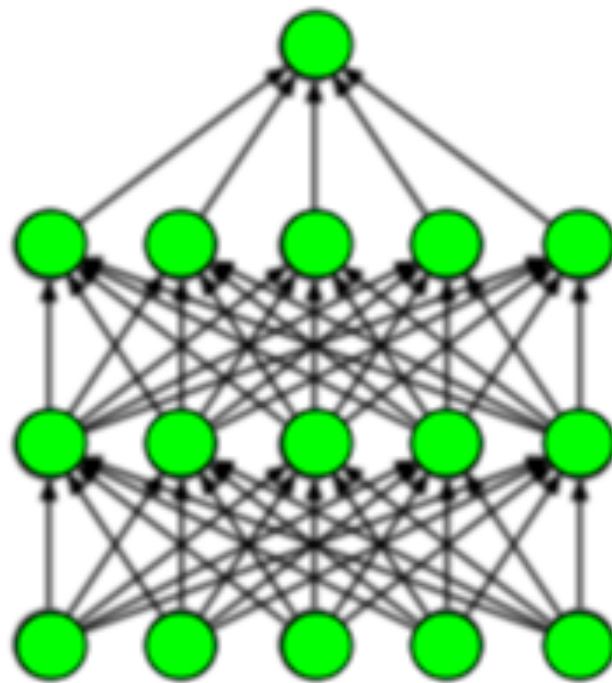
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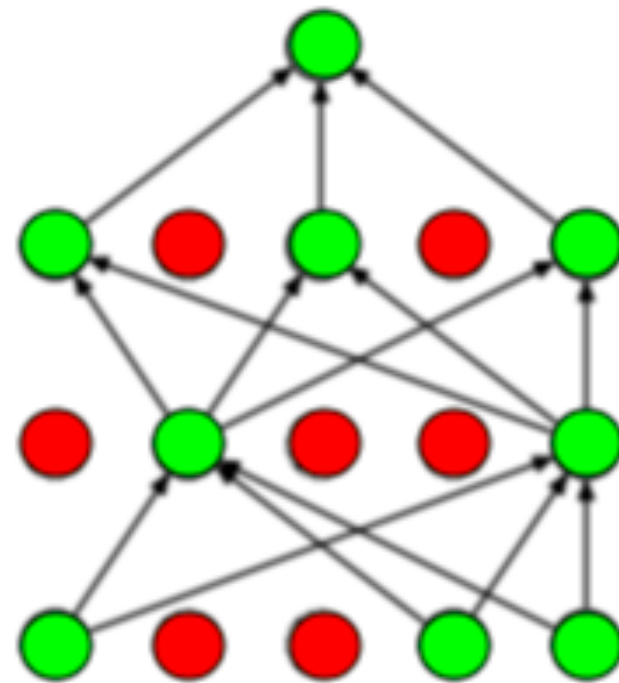
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# Taking care of Over-fitting: Dropouts



(a) Standard Neural Net



(b) After applying dropout.

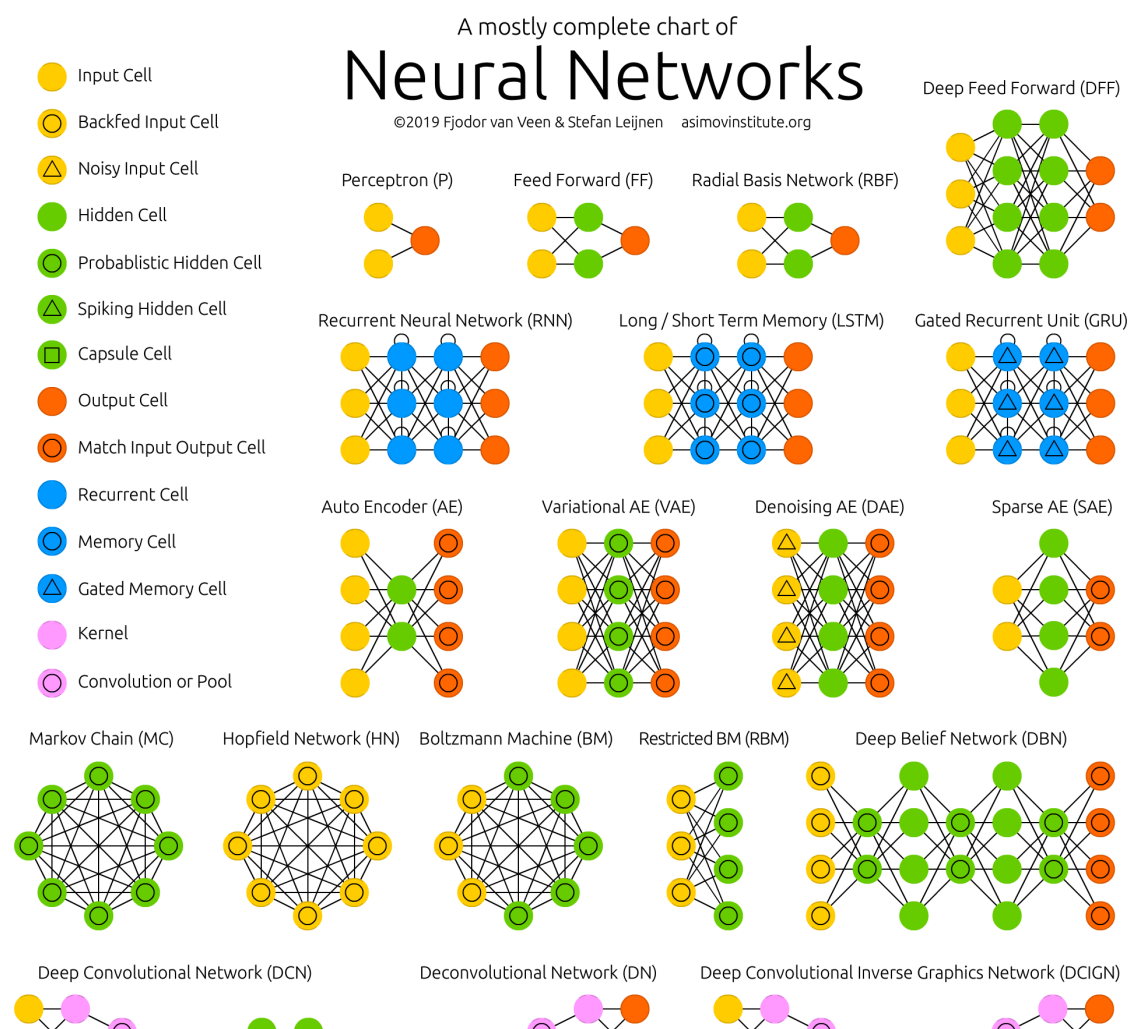
# Tensorflow Playground Demo

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# More DL Architectures

## Neural Networks Zoo

### Zoo Reference



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