

# Recommender Systems || Lecture 2

Summer 2022

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Univ. of Washington, Seattle

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# Motivation for Recommender Systems

- 1 Where you have a web based product sales, you need recommendations
- 2 Top companies deploy simple to sophisticated recommendation systems depending on their needs
- 3 Recommendations drives sales, revenue and customer base (e.g. Amazon)
- 4 Example: Amazon, Walmart, Facebook, YouTube, Twitter and so many more!
- 5 Scalability issues are rampant and bring in interesting solutions to Recommender systems
- 6 The course will discuss real case-studies and help students get hands on in thinking about building scalable recommender systems
- 7 The course will be focused on concepts and practical aspects of recommender systems. Hence all assessments will be through programming assignments and mini-projects hosted on Kaggle.

# Week by Week Break Down (Tentative)

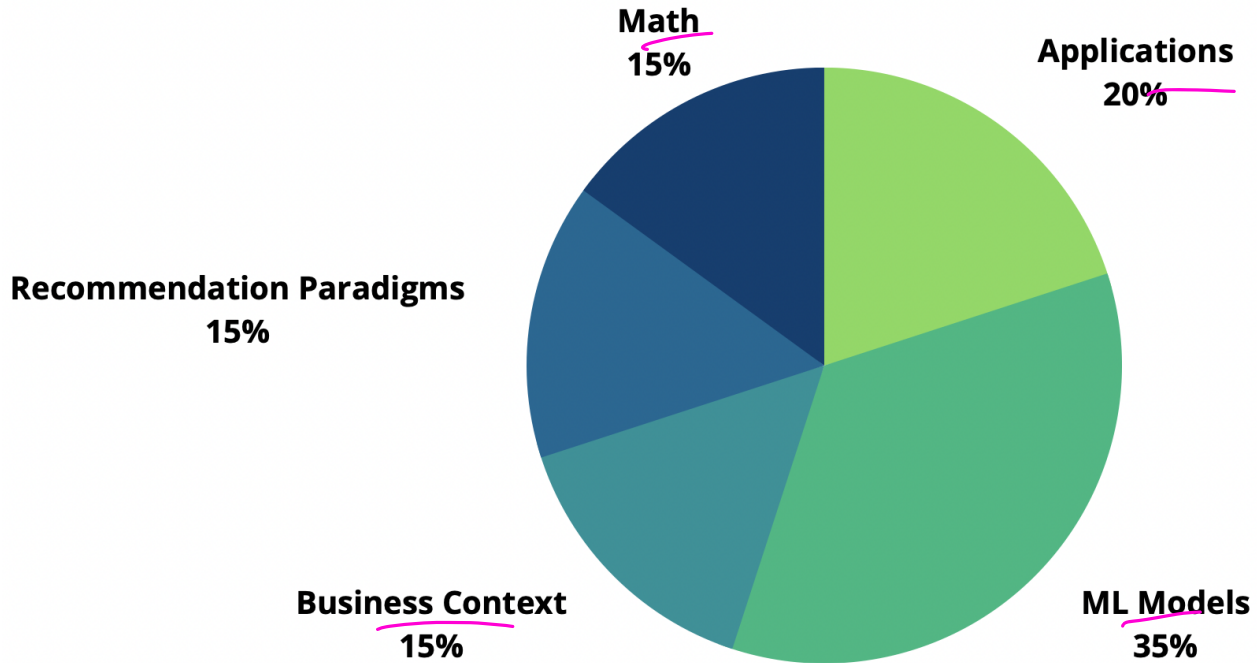
Week	Lecture Material	Assignment
1	Intro to Recommender Systems	Sambazon case study
2	Recommender System Baselines	Shopify case study
3	Matrix Factorization methods	Twitter case study
4	Matrix Factorization methods	Twitter case study
5	Deep Learning based recommendations	Walmart case study
6	ML Pipeline for Recommender systems	Amazon case study
7	Real-time Recommendations	Amazon Fresh case study
8	Diversity and Relevance	Final Project
9	Scaling Recommender systems	Final Project
10	Special Topics	Final Project

Summer!

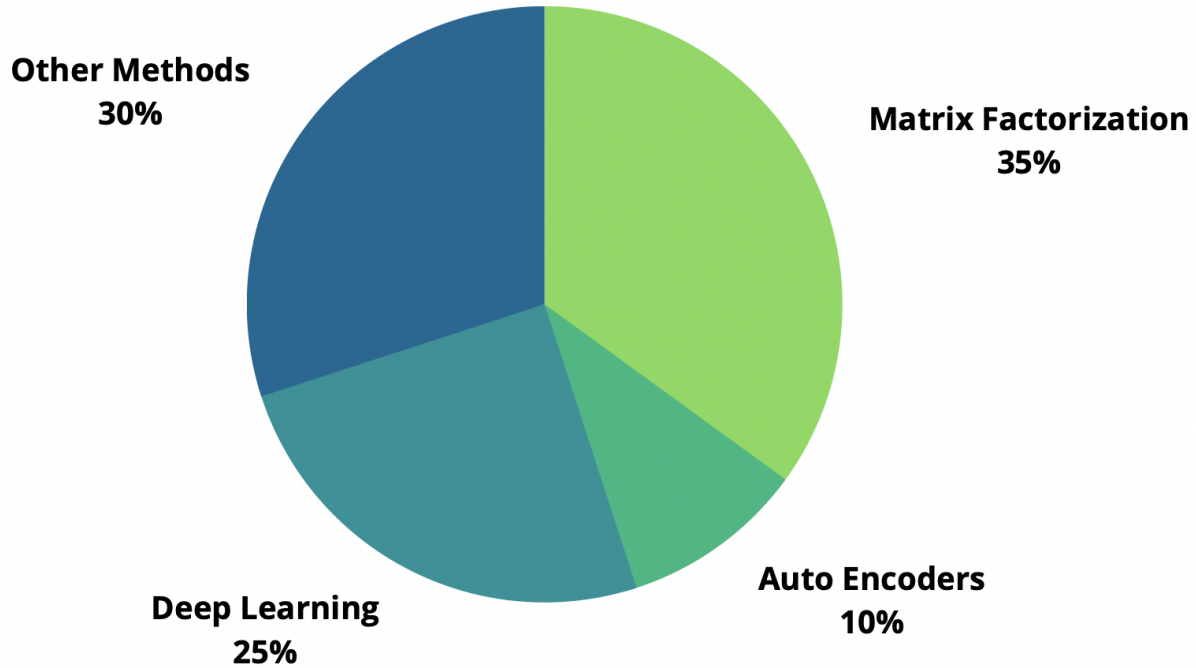
# Logistics

- Lectures on Monday and Wednesday 4 pm pst
- Monday lecture is in-person and Wednesday is online.
- **TA Quiz Section:** F: 4-5 PM (Zoom) → online
- **TA Office Hours:** Tu: 4-5 PM (EE 433 ~~Zoom~~) → in-person
- **Karthik Office Hours:** Monday 5 pm, EEB M258 / (unless indicated)  
Zoom

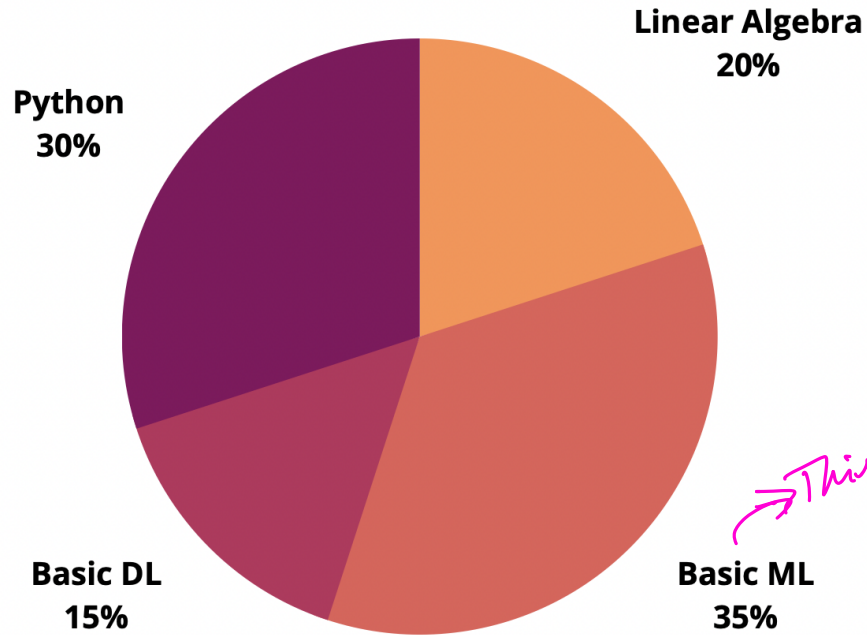
# Content



# ML Methods

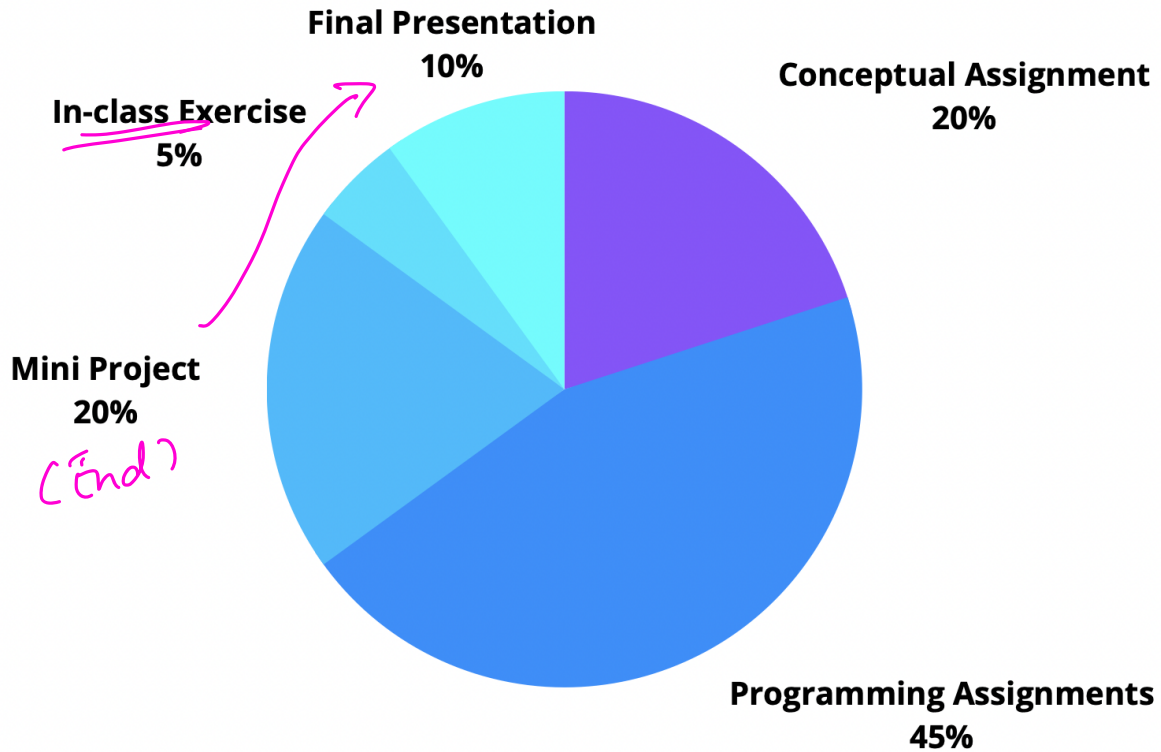


# Pre-requisites



*→ This is a requirement!  
(Catch up on your own)*

# Assessments





# Linear and Matrix Algebra Recap

Scalars & Vectors & Matrices & Tensors  
 $(\mathbb{R})$   $(\mathbb{R}^n)$   $(\mathbb{R}^m \times \mathbb{R}^n)$   $\rightarrow$   $(\mathbb{R}^m \times \mathbb{R}^n \times \mathbb{R}^d)$   
Complexity & dimensionality

vectors:  $p_1, p_2$

Add:  $p_1 + p_2$  (more frequently used)  
Multiply vectors:  $p_1 \cdot p_2 = p_1^T p_2$

$\square \quad \square \quad \square = \text{scalars!}$

2)  $p_1 \circ p_2 = \begin{bmatrix} \vdots \\ \vdots \\ \vdots \end{bmatrix} \begin{bmatrix} \vdots \\ \vdots \\ \vdots \end{bmatrix} = \begin{bmatrix} \vdots \\ \vdots \\ \vdots \end{bmatrix}$

(less used)  
Hadamard product

$$\|p_1\|_2^2 = p_1 \cdot p_1 = \begin{bmatrix} p_1^T \end{bmatrix} \begin{bmatrix} p_1 \end{bmatrix}$$

$$\|p_1\|_2 = \text{magnitude of } p_1 \\ = \sqrt{p_1 \cdot p_1}$$

$$\|X\|_F^2 = \langle X, X \rangle = X \cdot X \\ \text{Frobenius} \qquad \qquad \qquad = \text{Tr}(X^T X)$$

$$X \cdot Y = \text{Tr}(X^T Y)$$

$$\|X\|_F = \text{magnitude of matrix } X \\ = \sqrt{\text{Tr}(X^T X)}$$

$$\text{Tr}(Z) = ? = \text{Sum of diagonals of } Z \\ = z_{11} + z_{22} + z_{33} + \dots + z_{nn}$$

Example:-

$$Z = \begin{bmatrix} 1 & 4 & 5 \\ 2 & 7 & 8 \\ 9 & 3 & -2 \end{bmatrix}$$

$$\text{Tr}(Z) = ? \\ = 1 + 7 - 2 = 6$$

$$\|Z\|_F = \sqrt{\text{Tr}(Z^T Z)}$$

$$Z^T Z = ?$$

$$Z^T = \begin{bmatrix} 1 & 2 & 9 \\ 4 & 7 & 3 \\ 5 & 8 & -2 \end{bmatrix}$$

$$= \begin{bmatrix} \textcircled{1} & \textcircled{2} & \textcircled{9} \\ \textcircled{4} & \textcircled{7} & \textcircled{3} \\ \textcircled{5} & \textcircled{8} & \textcircled{-2} \end{bmatrix} \begin{bmatrix} \textcircled{1} & \textcircled{4} & \textcircled{5} \\ \textcircled{2} & \textcircled{7} & \textcircled{8} \\ \textcircled{9} & \textcircled{3} & \textcircled{-2} \end{bmatrix}$$

$Z^T$   $Z$

$$= \begin{bmatrix} 86 & & \\ & 74 & \\ & & 93 \end{bmatrix}$$

$$\text{Tr}(Z^T Z) = 253 = (86 + 74 + 93)$$

$$\|Z\|_F = \sqrt{253} \rightarrow \text{Frobenius norm of } Z$$

Euclidean norm of a vector  $\Leftrightarrow$  Frobenius norm of a matrix.

# Application of matrix

Dot products??

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→ Image Search  $\rightarrow I_1, I_2$

→ Image Similarity  $\rightarrow \underline{I_1}, \underline{I_2}$

→ Image Distance

$$\|I_1 - I_2\|_F$$

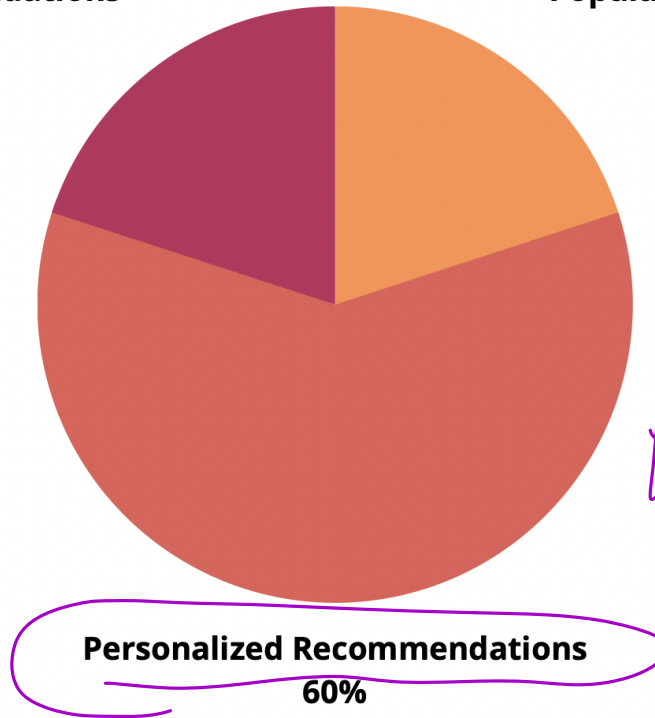
↓  
Distance between  $I_1$  &  $I_2$ !

# Introduction to Recommender Systems

# Recommender Types

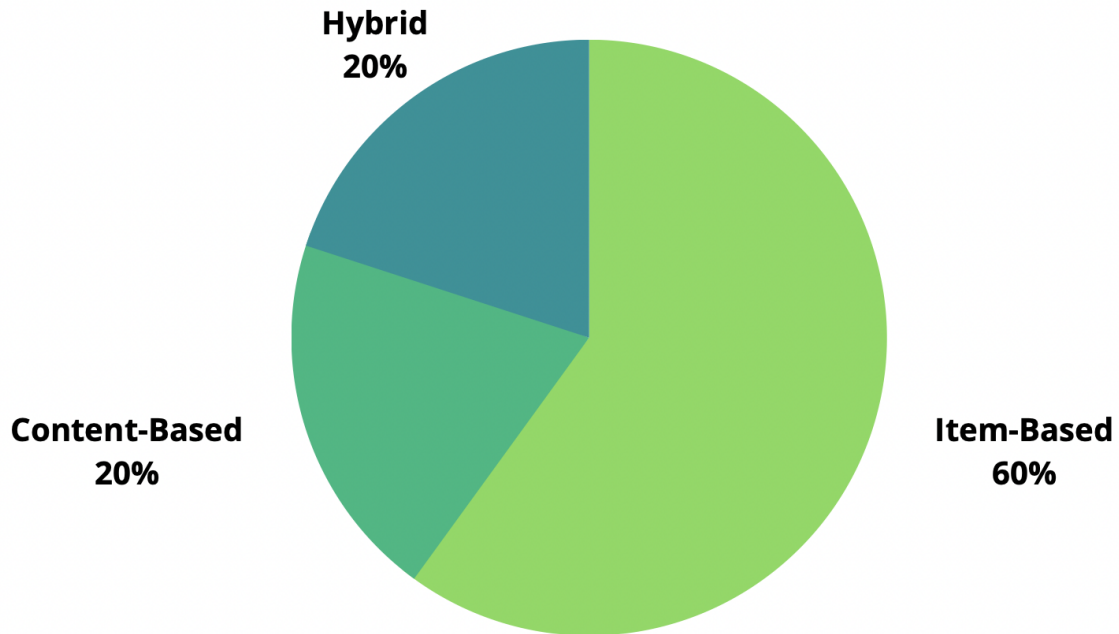
**Cold-start Recommendations**  
20%

**Popular Recommendations**  
20%



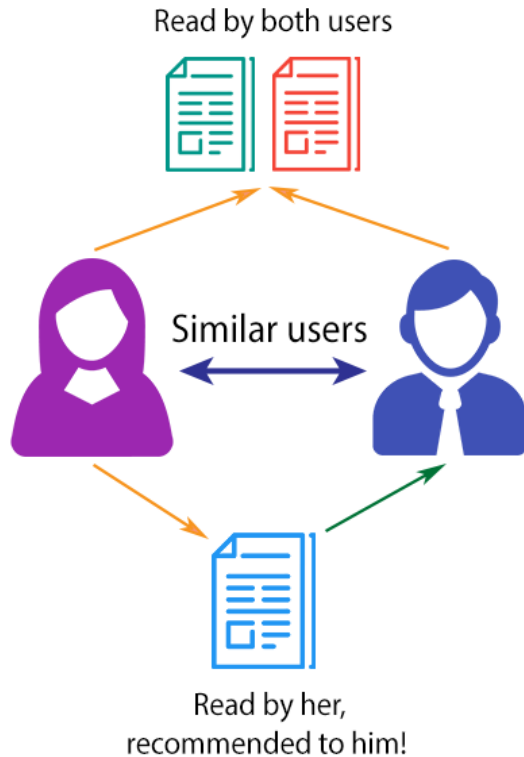
**Personalized Recommendations**  
60%

# Recommenders

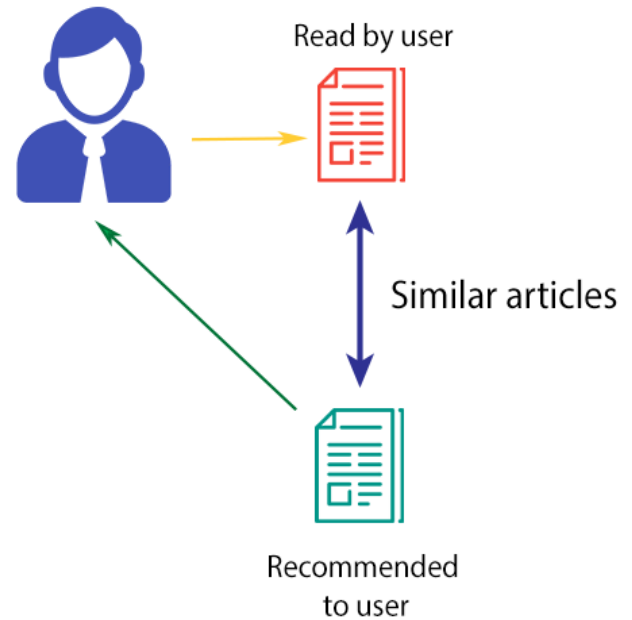


# Collaborative filtering

## COLLABORATIVE FILTERING



## CONTENT-BASED FILTERING





# Item based recommendations

amazon.com

Recommended for You

Amazon.com has new recommendations for you based on [items](#) you purchased or told us you own.



[Google Apps Deciphered: Compute in the Cloud to Streamline Your Desktop](#)

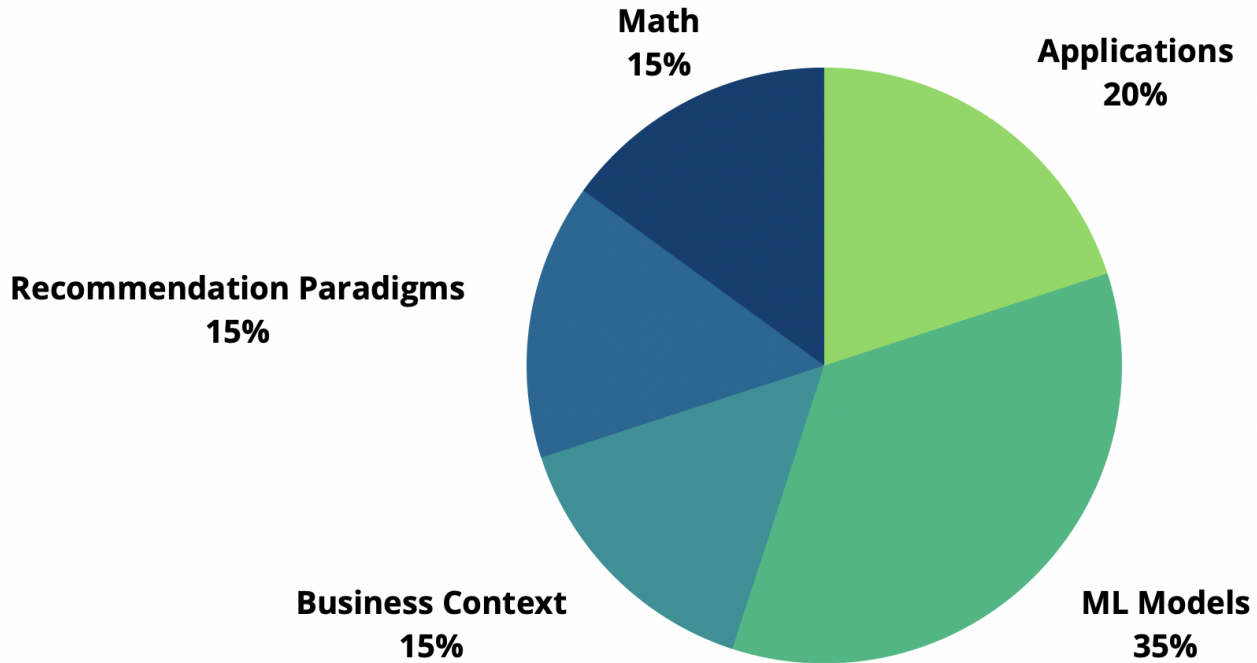


[Google Apps Administrator Guide: A Private-Label Web Workspace](#)



[Googlepedia: The Ultimate Google Resource \(3rd Edition\)](#)

# Content



# Amazon Recommendations

Explore the Amazon Webpage

[Amazon home page](#)

# Identifying the types of recommendations

(widgets)

- 1 Past incomplete purchase recs

# Identifying the types of recommendations

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- 2 Buy it again recs

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- ④ Customers who bought this also bought
- ⑤ Similar items to items viewed recs



# Identifying the types of recommendations

- 1 Past incomplete purchase recs
- 2 Buy it again recs
- 3 Frequently bought recs
- 4 Customers who bought this also bought
- 5 Similar items to items viewed recs
- 6 Similar items to items purchased recs

# Recommendation systems modeling

- 1 Goal may not be building one 'ultimate' recommender widget

# Recommendation systems modeling

- ① Goal may not be building one 'ultimate' recommender widget
- ② Variety of widgets might get better bang for the buck as we saw in earlier example

# Breakout discussion #1

## Evaluating widgets


(Statistical) 2: (A/B testing) → online / Live Testing  
1: offline testing → Post data

You are working in a team of engineers, data scientists and UX designers on a new home page for fashion products. As an ML engineer, you want to build out recommendation widgets on your fashion homepage to help customers find fashion products faster. You decide that you want to have 10 different widgets for different channels of recommendations on the home page to help customers and also maximize sales. The UX designer you work with says that would be not fit with their design specs and asks you to limit it to 3 widgets. Your manager asks you and the UX designer to come to consensus so the team can proceed with execution. What steps/data driven arguments would you take and/or make to resolve this situation or come to a consensus that best meets the common goals that your team has for the home page?

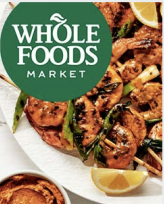
(metrics)

# Widgets Example

Savor and save on exciting deals this Prime Day. [Learn more >](#)



Ignite grilling season >




WHOLE FOODS MARKET


This week's best deals >

Price as marked. While supplies last.








Shop by dietary preference >










SALE










**Buy it again** [See all past purchases >](#)

 <p>365 by Whole Foods Market, Mi... ★★★★ 15,285 <a href="#">Add to Cart</a></p>	 <p>Organic Banana ★★★★ 18,071 \$0.79/lb <a href="#">Add to Cart</a></p>	 <p>Honeydew Melon ★★★★ 4,075 \$4.99 <a href="#">Add to Cart</a></p>	 <p>Vita Coco, Coconut Water, 33.8 Fl Oz ★★★★ 6,776 <a href="#">Add to Cart</a></p>	 <p>Herb Cilantro Organic, 1 Bunch ★★★★ 18,441 <a href="#">Add to Cart</a></p>	 <p>365 by Whole Foods Market, St... ★★★★ 6,531 <a href="#">Add to Cart</a></p>	 <p>365 by Whole Foods Market, Ch... ★★★★ 4,908 <a href="#">Add to Cart</a></p>
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**Pick up where you left off** [Page 1 of 3](#)

 <p>Organic Plum Roma Tomato ★★★★ 2,617 <a href="#">Add to Cart</a></p>	 <p>Organic Loose Red Beets ★★★★ 4,911 <a href="#">Add to Cart</a></p>	 <p>Organic Ginger Root ★★★★ 15,728 <a href="#">Add to Cart</a></p>	 <p>Organic Red Bell Pepper ★★★★ 3,822 <a href="#">Add to Cart</a></p>	 <p>Organic Yellow Bell Pepper ★★★★ 5,208 <a href="#">Add to Cart</a></p>	 <p>Organic D'Anjou Pear ★★★★ 6,748 <a href="#">Add to Cart</a></p>	 <p>Organic Tomato On-The-Vine ★★★★ 18,166 <a href="#">Add to Cart</a></p>
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**Produce** [See Produce >](#)

 <p>Organic Romaine Hearts, 3ct ★★★★ 22,240 \$4.99 <a href="#">Add to Cart</a></p>	 <p>365 by Whole Foods Market, Sa... \$5.99 <a href="#">Add to Cart</a></p>	 <p>Green Bell Pepper ★★★★ 31,778 \$2.49/lb <a href="#">Add to Cart</a></p>	 <p>Navel Orange ★★★★ 16,111 \$1.99/lb <a href="#">Add to Cart</a></p>	 <p>Red Bell Pepper ★★★★ 2,900 \$3.49/lb <a href="#">Add to Cart</a></p>	 <p>Shallot ★★★★ 1,458 \$3.99/lb <a href="#">Add to Cart</a></p>	 <p>Organic Blackberries, 6 oz ★★★★ 10,497 \$3.00 \$4.99 <a href="#">Add to Cart</a></p>
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*widgets carousel*

# Simple Baseline Recommender

## Cosine Similarity

Let's say you want to recommend products from some categories (e.g. groceries, music and fitness to customers) in a way that is personalized and so they find it relevant. Here's a simple baseline model:

- 1 **Representation:** Find a way to represent your product by a fixed length vector of some dimension  $d$ .  $d$  here usually captures the number of relevant "features".

↙  
OoOoMation (Tensor)  
→


# Simple Baseline Recommender

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- 2 **Cosine Similarity:** Let's say you have a reference product  $p$  and candidate products to recommend  $p_1, p_2, \dots$ . Evaluate the cosine similarity between product  $p$  and all the other products.

$p \rightarrow \text{Ear phones } (p)$   
 $p_1 \rightarrow \text{Another 1 } (p_1)$   
 $p_2 \rightarrow \text{Watch } (p_2)$



Purchase

# Simple Baseline Recommender

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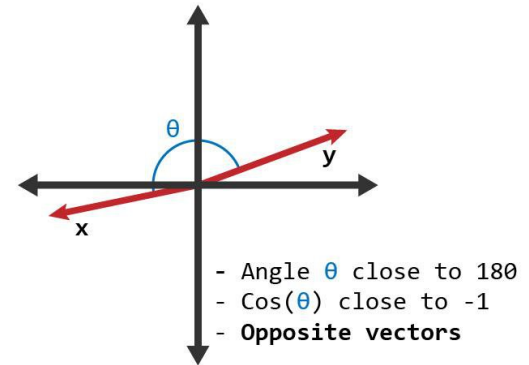
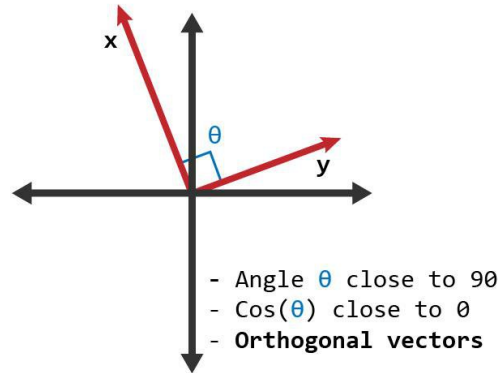
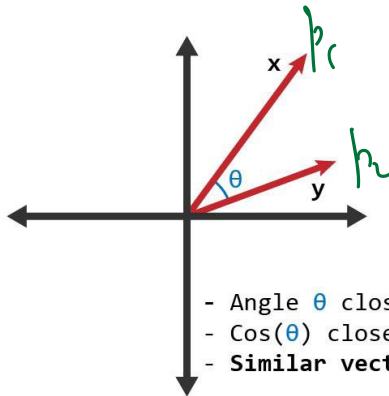
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- 3 **Rank:** Rank the candidates for recommendation based on cosine similarity scores (highest to lowest).
- 4 **Truncate:** Pick top  $k$  from the ranked list to recommend. Where  $k$  is usually decided by specifications of your recommender widget.

# Cosine Similarity

## Definition

Let's say we have two vectors  $p_1, p_2$ . The cosine similarity between the two vectors is given by:  $\frac{p_1 \cdot p_2}{\|p_1\|_2 \|p_2\|_2} = \cos(\theta)$

-1 & 1



## Image reference

# ICE #1

## Cosine Similarity

Poll

Let's say we have 3 products with attributes as fitness (0 or 1), groceries (0 or 1) and music (0 or 1). Each product can now be represented by a 3 dimensional binary vector. Let  $P1 = [0, 1, 1]$ ,  $P2 = [1, 1, 0]$ ,  $P3 = [1, 0, 0]$ . If a customer has bought  $P1$ , you want your baseline recommender to pick between  $P2$  and  $P3$  as your next recommendation for the customer. You do this by evaluating cosine similarities between the appropriate products. The resulting similarities ~~that~~ will be used ~~compared~~ for the purpose of making a recommendation are as follows:

- 1 [0, 0.5]
- 2 [0.5, 0.71]
- 3 [0.71, 0]
- 4 None of the above

$$\cos(\underline{P_1}, \underline{P_2}) \quad \xrightarrow{\text{reference product}} \quad \cos(\underline{P_1}, \underline{P_3})$$

$$= \frac{[0, 1, 1] \cdot [1, 1, 0]}{\| \quad \|_2 \quad \| \quad \|_2}$$

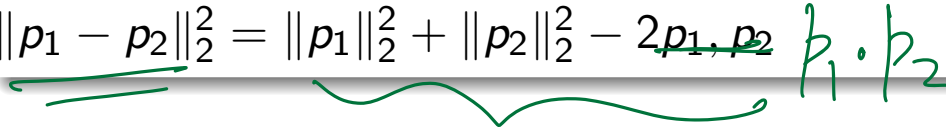
$$\hookrightarrow \frac{[0, 1, 1] \cdot [0, 0, 0]}{\| \cdot \|_2 \quad \| \cdot \|_2} = 0$$

$$= \frac{1}{\sqrt{2} \sqrt{2}} = \underline{\underline{\frac{1}{2} = 0.5}}$$

# Connecting Similarity with Distance

## Euclidean Distance

Euclidean distance between two vectors  $p_1$  and  $p_2$  is given by

$$\|p_1 - p_2\|_2^2 = \|p_1\|_2^2 + \|p_2\|_2^2 - 2p_1 \cdot p_2$$


# Connecting Similarity with Distance

## Euclidean Distance

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$$\|p_1 - p_2\|_2^2 = \|p_1\|_2^2 + \|p_2\|_2^2 - 2p_1 \cdot p_2$$

## Euclidean Distance with normalization

Assume that representation of two products  $p_1$  and  $p_2$  are normalized so that  $\|p_1\|_2$  and  $\|p_2\|_2$  are equal to 1. Then,

$$\begin{aligned} \|p_1 - p_2\|_2^2 &= \underbrace{1} + \underbrace{1} - \underbrace{2p_1 \cdot p_2}_{\|p_1\|_2 \|p_2\|_2} \\ &= 2 - 2 \times \text{Cosine Similarity} \\ &\sim 1 - \text{Cosine Similarity} \end{aligned}$$

$$\boxed{\text{dist}^2 \propto 1 - \text{Cosine Similarity}}$$

# Connecting Similarity with Distance

## Euclidean Distance

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$$\|p_1 - p_2\|_2^2 = 1 + 1 - 2p_1 \cdot p_2$$

= 2 - 2 × Cosine Similarity

~ 1 - Cosine Similarity

So with normalization of vectors, distance between products is proportional to 1 minus the similarity between products

# Connecting Similarity with Distance

## Euclidean Distance

Euclidean distance between two vectors  $p_1$  and  $p_2$  is given by

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= 2 - 2 × Cosine Similarity

~ 1 - Cosine Similarity

So with normalization of vectors, distance between products is proportional to 1 minus the similarity between products  
Higher the similarity, lower the distance and vice versa.





## ICE #2

$$\text{dist}^2 = \|\mathbf{r}_1 - \mathbf{r}_2\|_2^2 = 2 - 2 \times \text{wine similarity}$$

### Bounds on distance

Let's say we want to find the distance between two products  $p_1$  and  $p_2$ . Assume that the vector representation of these products is normalized, i.e.  $\|p_1\|_2 = \|p_2\|_2 = 1$ . What can you say about the bounds on distance between  $p_1, p_2$ , i.e.  $\|p_1 - p_2\|_2$ ?

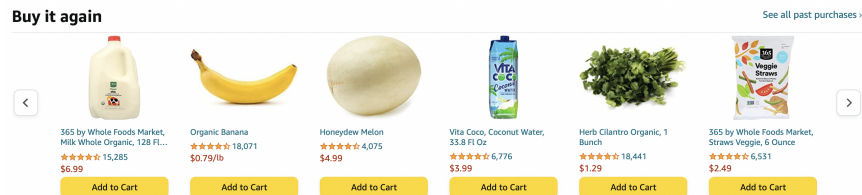
- 1 Between 0 and 1
- 2 Between -1 and 1
- 3 Between 0 and 2
- 4 Between -1 and  $\sqrt{2}$

# Breakout discussion #2

(Come back later)

## Repeat purchase recommendations

Assume you are working in a team at Sambazon that is building a repeat purchase recommender system. You have access to anonymized data on customers past purchase history over the past year for popular categories of products. What would be a simple baseline model for repeat purchase recommendations? What factors would you consider when you design your baseline model (your factors have to tie in with the bottom line/top line metrics that your team/project cares about) How would you evaluate the goodness of your model? What specific quantitative metrics would you use to measure the goodness? What are the pros/cons of your baseline and how would you improve it?



# Behavioral vs Content Based Recommendations

- 1 **Behavioral:** Recommendations on understanding customer behaviors based on data (purchases, views and other data).  
**Collaborative Filtering** is a modeling approach in recommendations that is solely dependent on behavioral data.  
*Customers who bought this also bought this..* is an example of a behavioral recommender.
- 2 **Content:** Recommenders that use content information on items or products are called content based recommenders.  
*Items similar to what you purchased ...* is an example of this.
- 3 **Hybrid:** Often times, a mixture of behavioral and content based data leads to better overall recommender widgets.

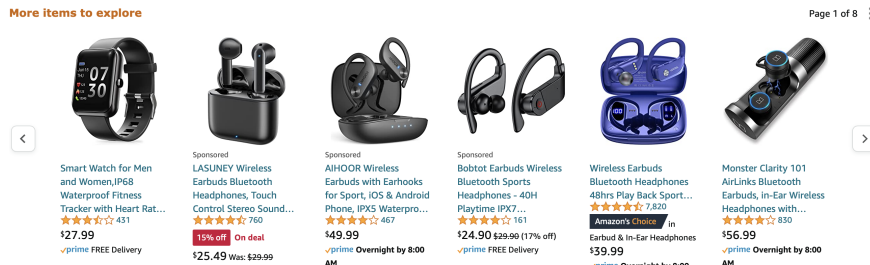
Main signal:- Behavior  
Secondary Signal:- Content

# Breakout discussion #3

## Customers who bought this also bought ...

Assume that your team would like you to build a baseline recommender for a newly launched fashion product line of the type, “Customers who bought this also bought ...” Your UX designer mentions that you can only surface 5 products at a time on the widget you are building. Discuss and outline step by step how you would arrive at the top 5 products to surface given a single fashion product as input. What if now the input is 3 past fashion purchases of the customer instead of one? How do you convince your team that your widget is doing well enough to be considered for a live launch? How do you evaluate your widget performance when you go live and launch it?

Back Test  
A/B



# Content based recommendations

- 1 Use features (or content) from the products to make recommendations.



# Content based recommendations

- 1 Use features (or content) from the products to make recommendations.
- 2 This includes product categories and product brand

Related to items you've viewed [See more](#)



# Content based recommendations

- 1 Use features (or content) from the products to make recommendations.
- 2 This includes product categories and product brand
- 3 Anything else? | *hash tags, keywords, description*

Related to items you've viewed [See more](#)



# Breakout discussion #4

## New product on the block

Your team is launching new products and product categories to the massive product line of Sambazon. You are the new data scientist hired to surface these new products to customers so your team can drive the sales for the launched products. As of now, there is no easy way for a customer to see the new products, as it isn't yet popular and also because the new products have very little sales to be surfaced by other widgets that exist on the Sambazon recommendations pipeline. How would you leverage what you know about the new product line including any product descriptions and meta data to drive up the sales for the products. Assume the new products are in a product category that a significant percentage of Sambazon customers have purchased from in the past. Come up with a clear step-by-step model/algorithm/approach and also discuss how you will evaluate your recommender model?



# Next Lecture

- SVD based recommendations
  - Other baseline methods for recommendations
  - Introduction to Matrix Factorization
- 